

PHYS 3038 Optics

L8 More on Geometrical Optics

Reading Material: Ch6.3-6.5



Shengwang Du



2015, the Year of Light

6.3 Aberrations

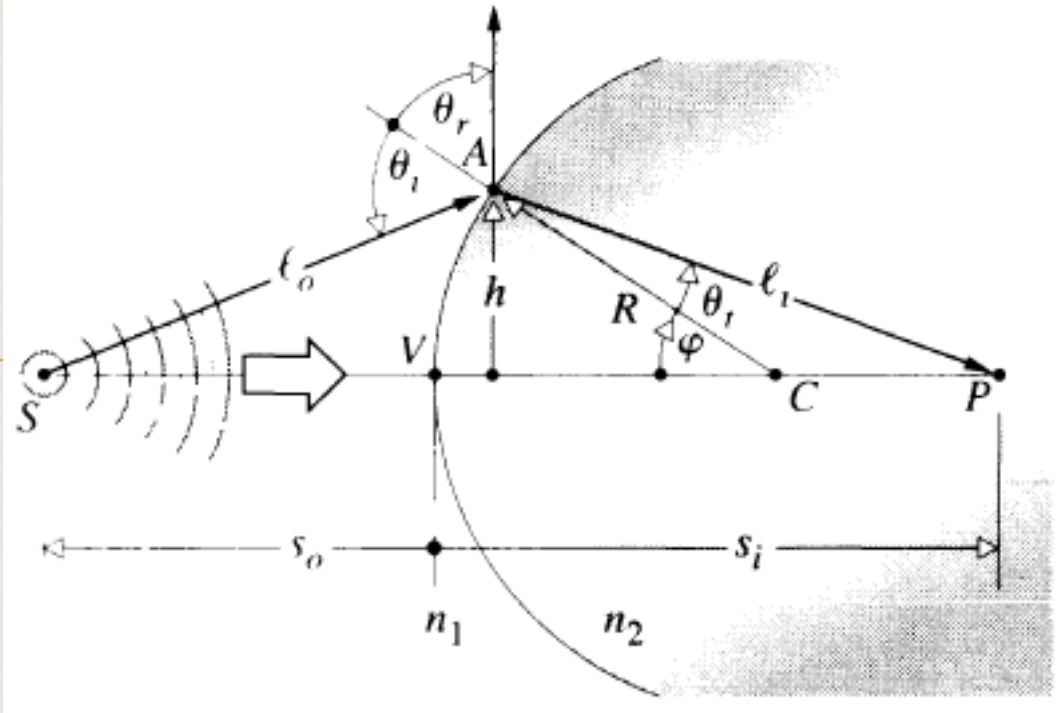


❧ Monochromatic aberrations

- ❧ Spherical aberration
- ❧ Coma
- ❧ Astigmatism
- ❧ Field curvature
- ❧ Distortion

❧ Chromatic aberrations

Spherical Aberration



Paraxial condition $\sin \varphi \cong \varphi$

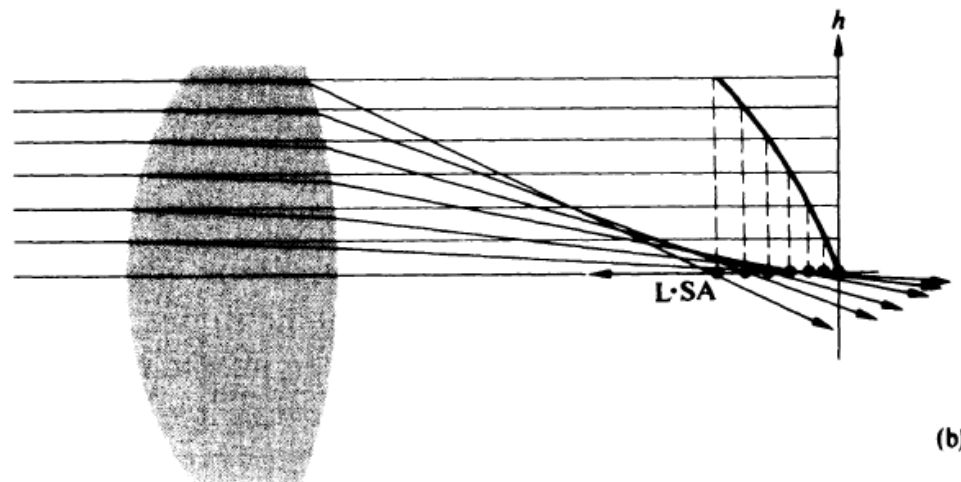
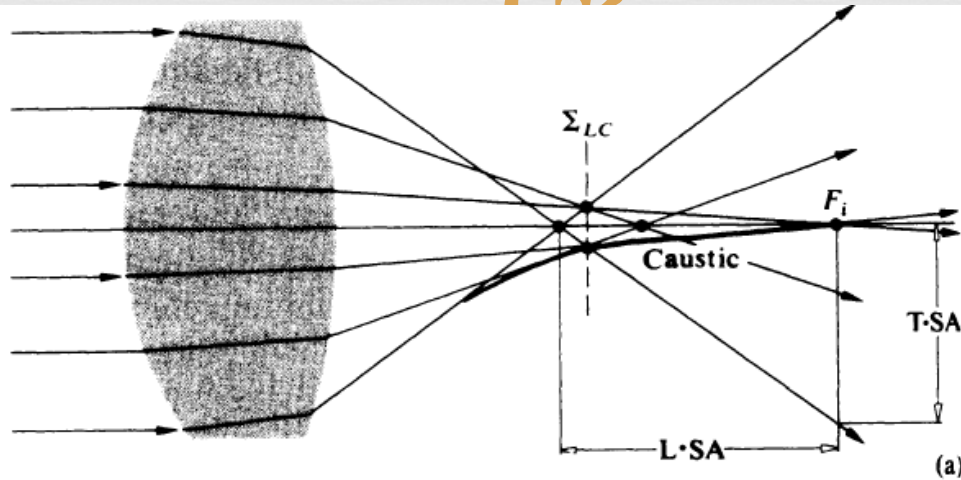
$$\frac{n_1}{S_o} + \frac{n_2}{S_1} = \frac{n_2 - n_1}{R}$$

$$\sin \varphi = \varphi - \frac{\varphi^3}{3!} + \frac{\varphi^5}{5!} - \frac{\varphi^7}{7!} + \dots$$

$$\frac{n_1}{S_o} + \frac{n_2}{S_1} = \frac{n_2 - n_1}{R} + h^2 \left[\frac{n_1}{2S_o} \left(\frac{1}{S_o} + \frac{1}{R} \right)^2 + \frac{n_2}{2S_i} \left(\frac{1}{R} - \frac{1}{S_i} \right)^2 \right]$$

L.SA & T.SA

CA



Wavefront Aberration

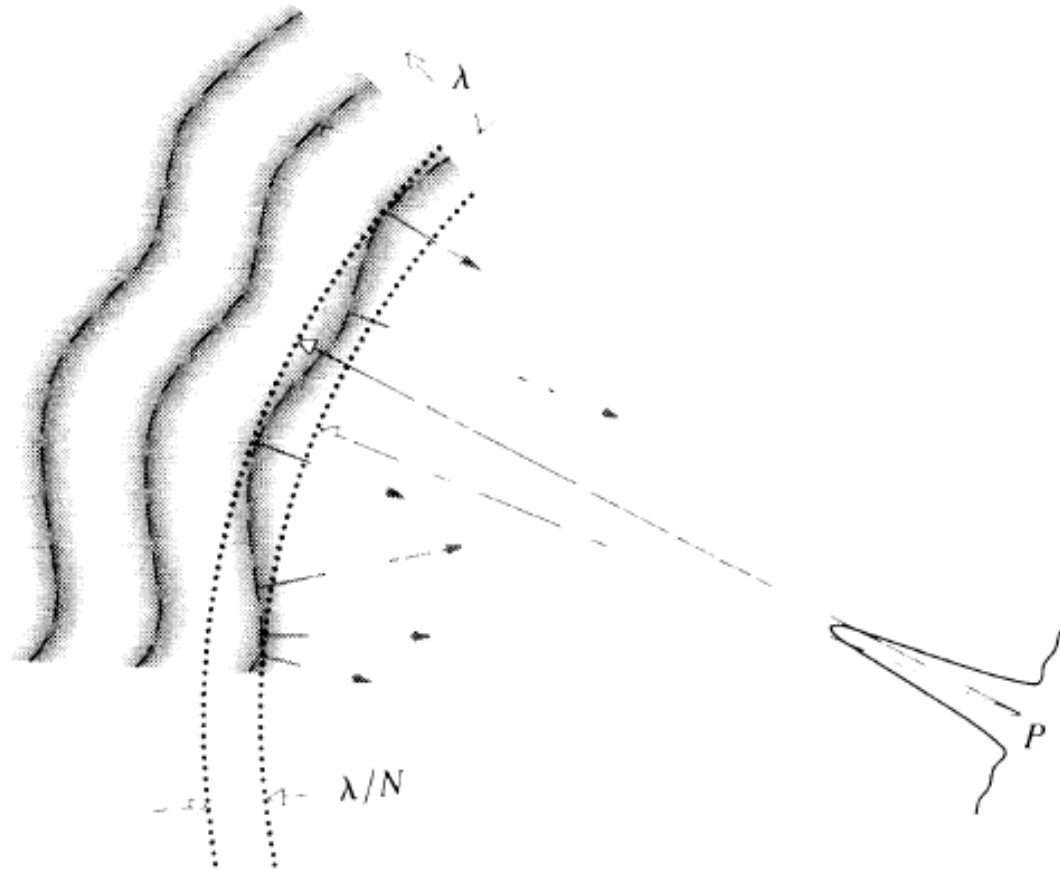
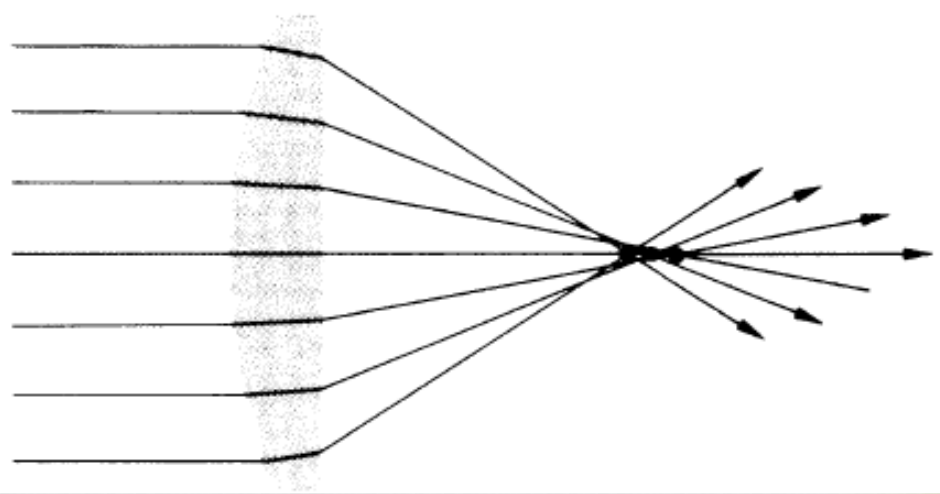
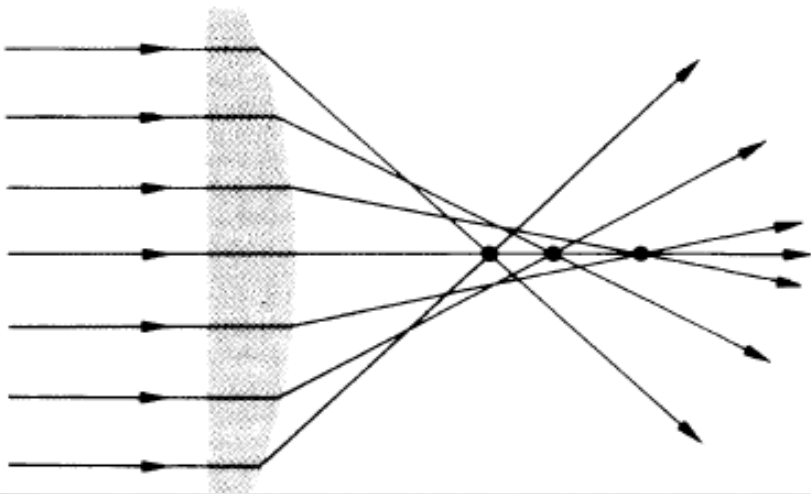


Figure 6.15 Since this wavefront deviates from a portion of a sphere (converging to the Gaussian image point), it is said to be aberrated. The extent of that deviation measured peak-to-peak is an indication of how far from perfection the image will be.

Lens Alignment for minimizing SA



Huygens Points

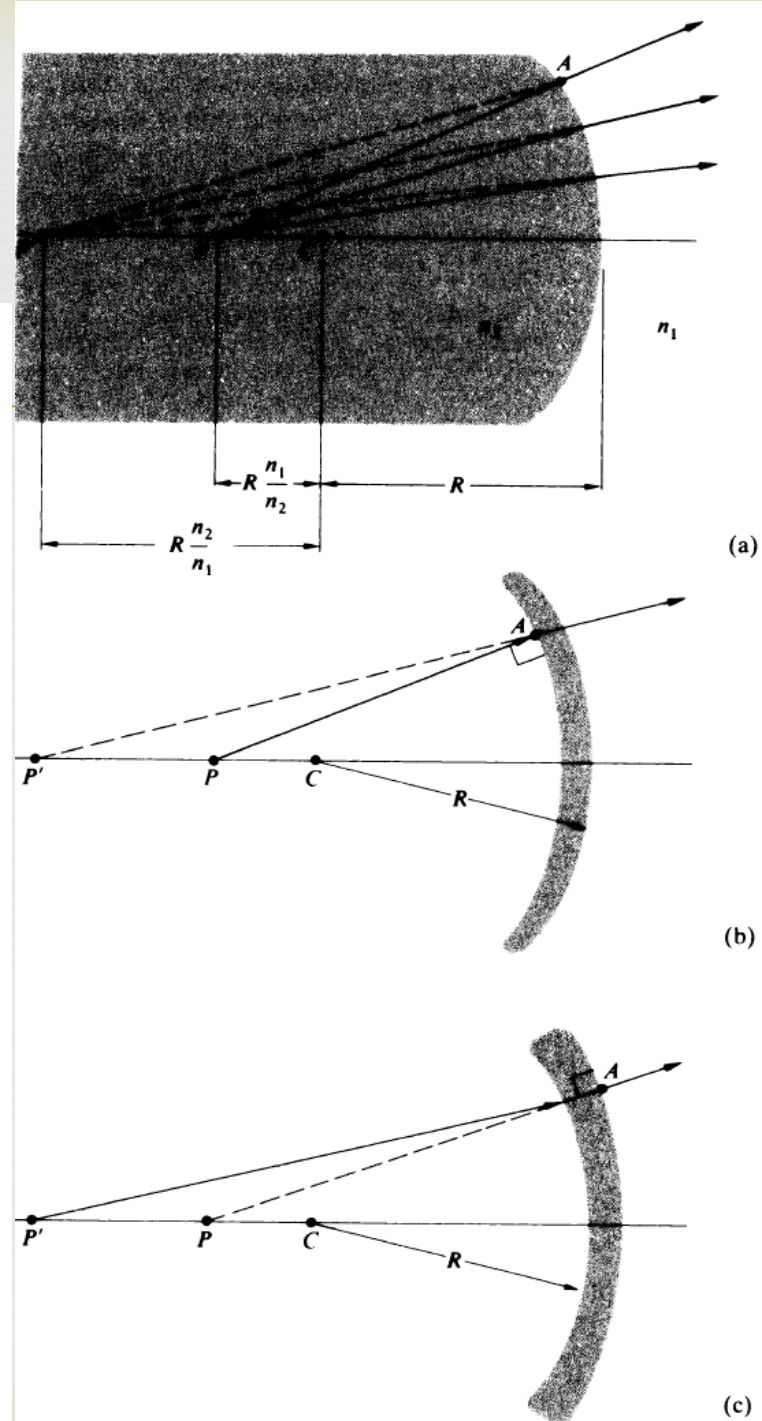
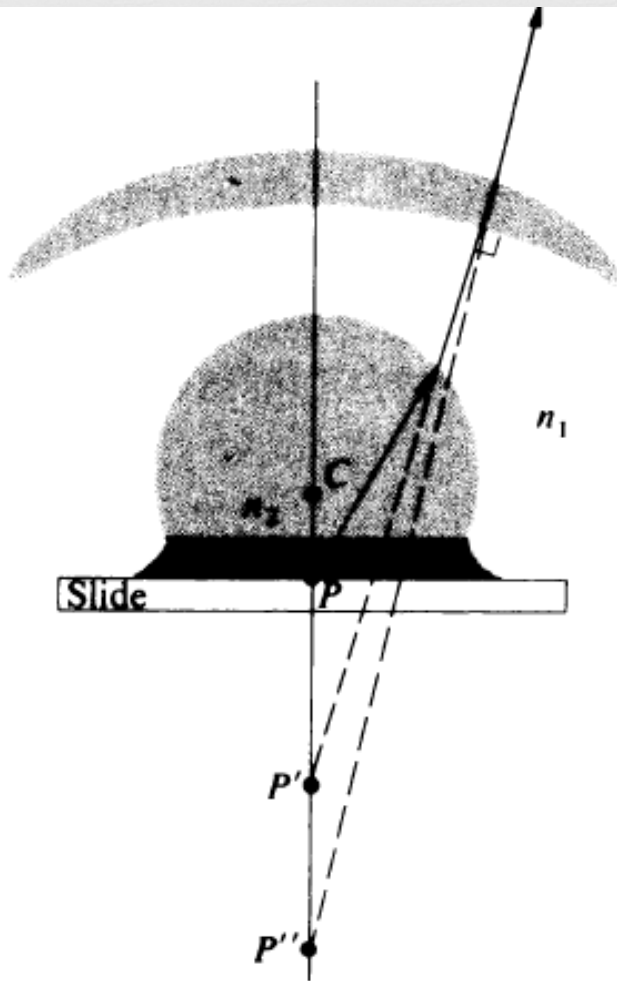
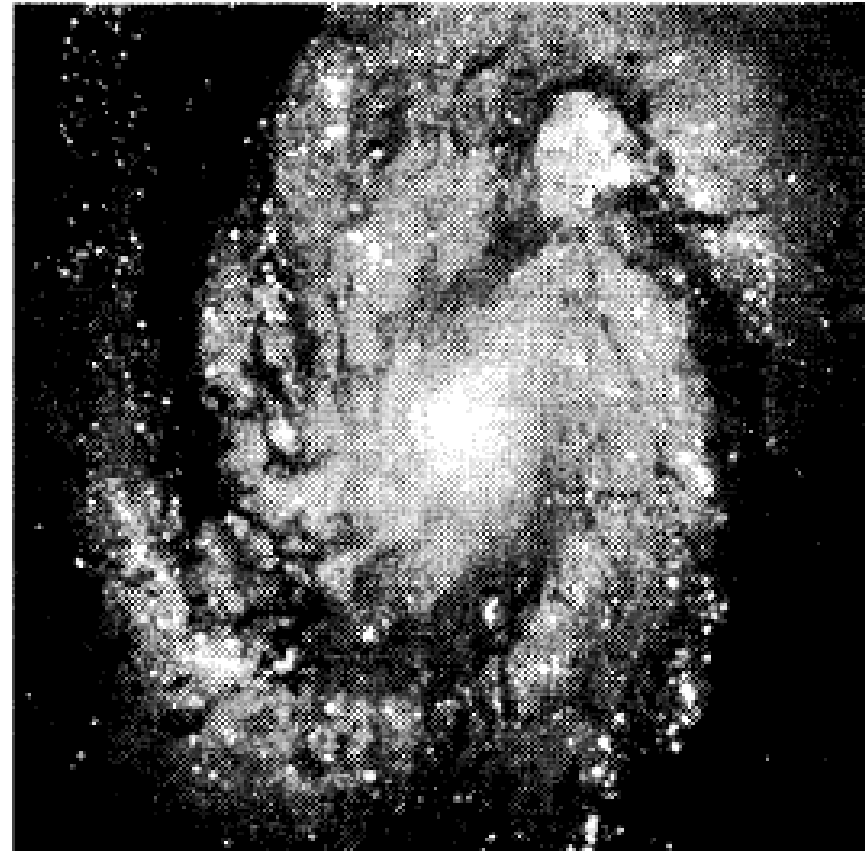
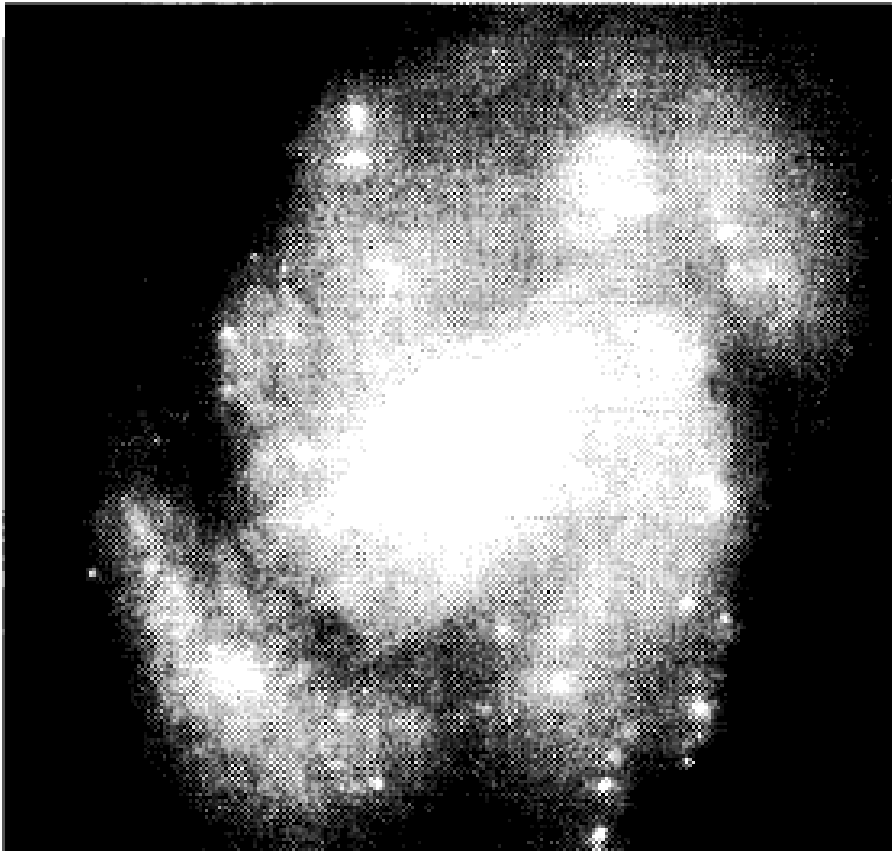


Figure 6.18 An oil-immersion microscope objective.

Hubble Telescope

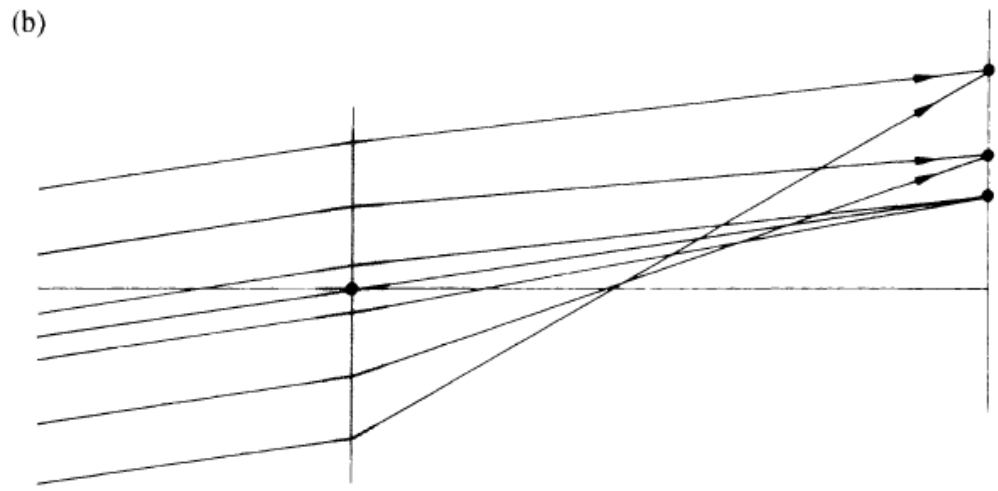
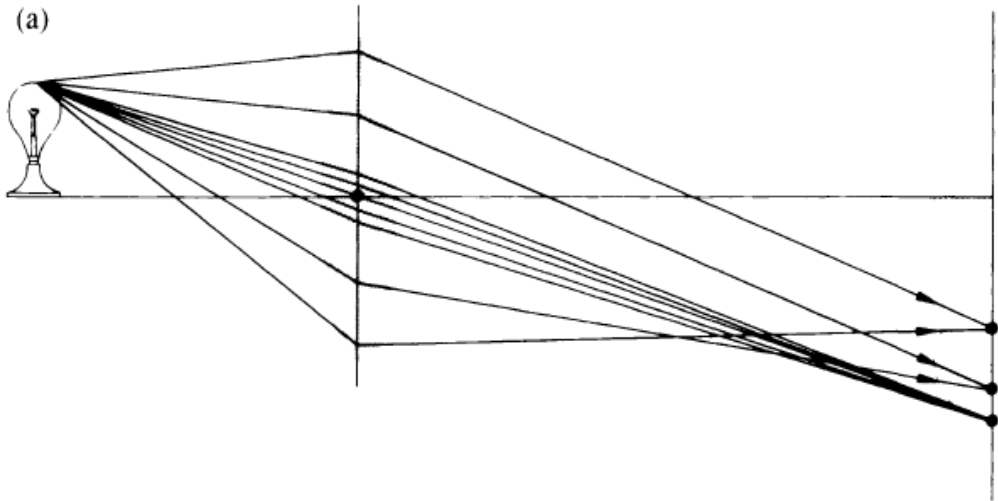


Hubble Telescope

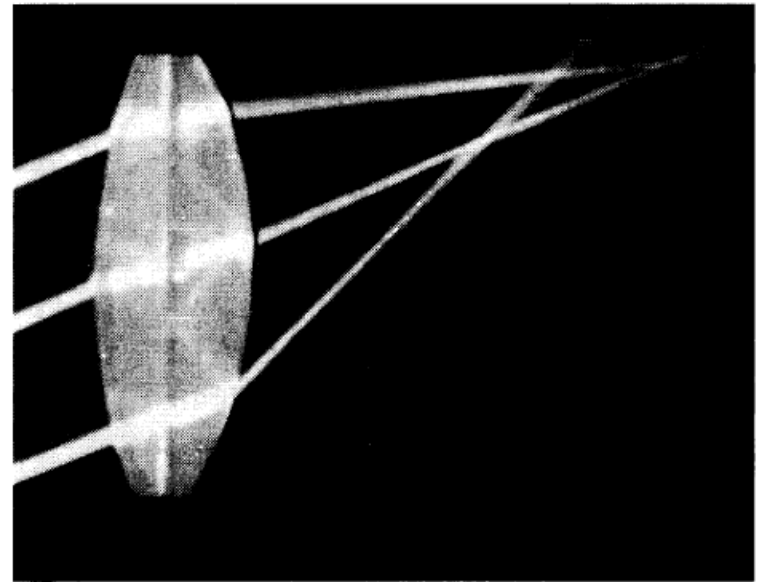


HST images of the M-100 galaxy with (before repair) and without (after repair) spherical aberration. (Photos courtesy of NASA.)

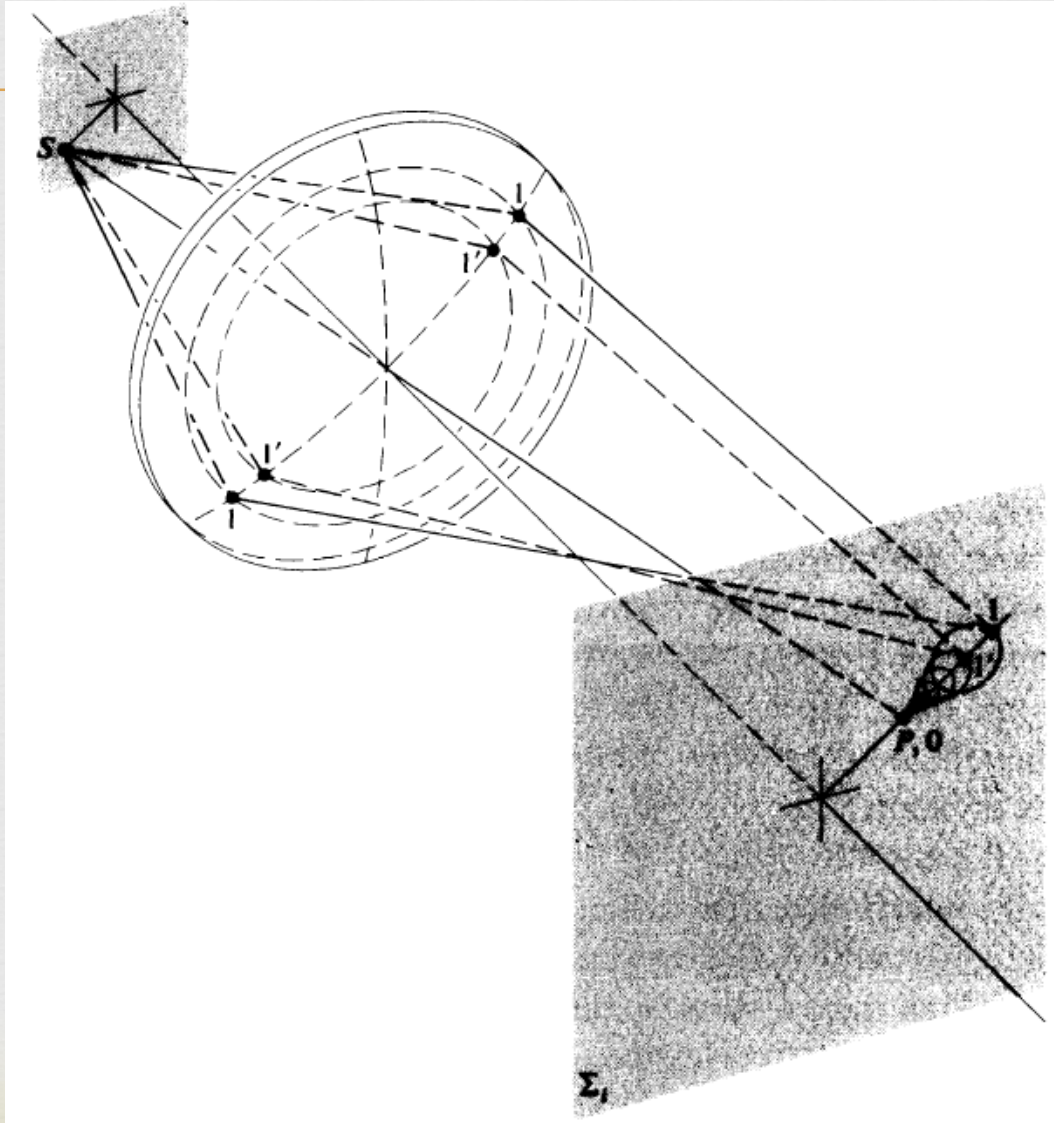
Coma



(c)



Coma



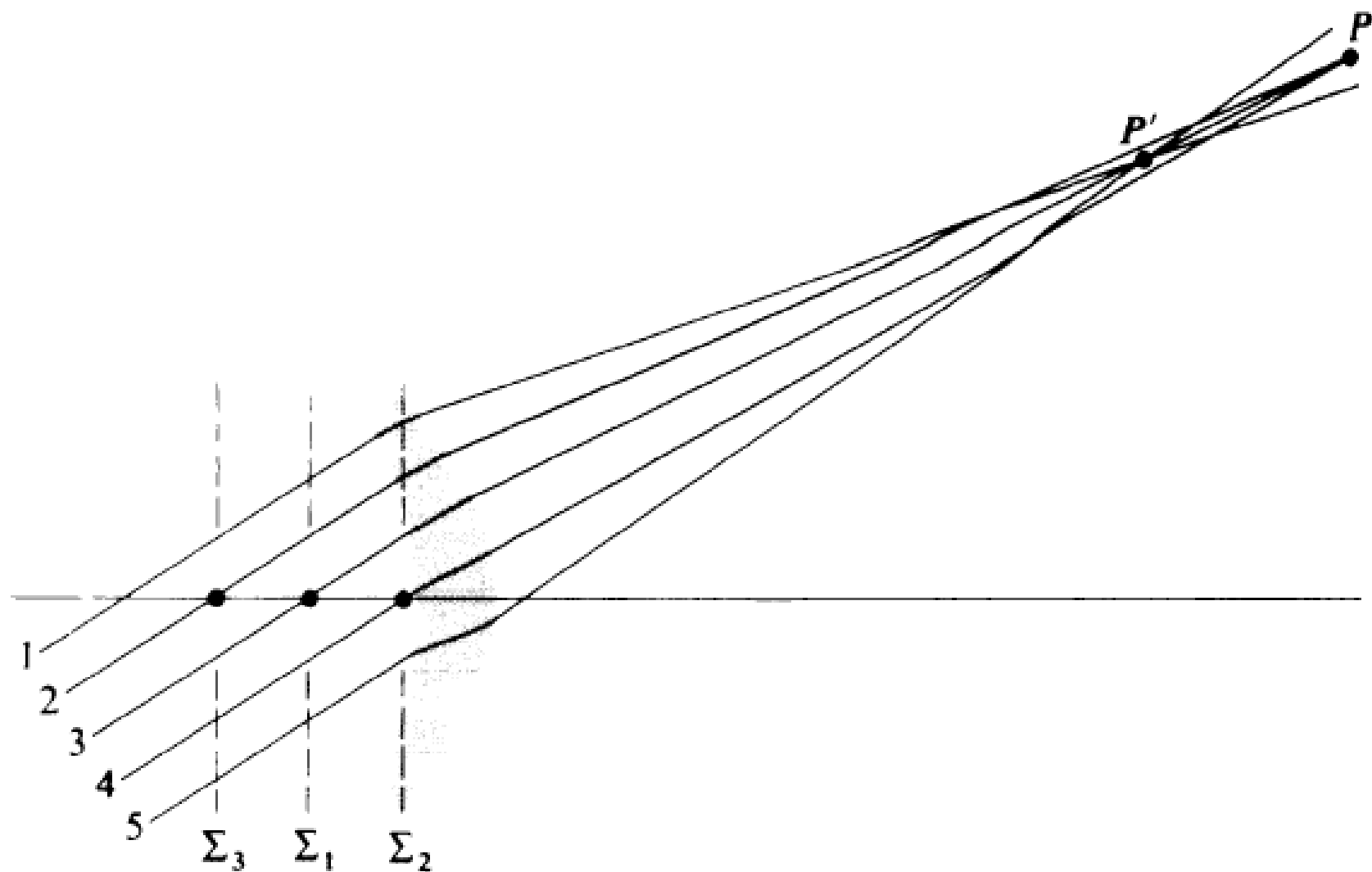
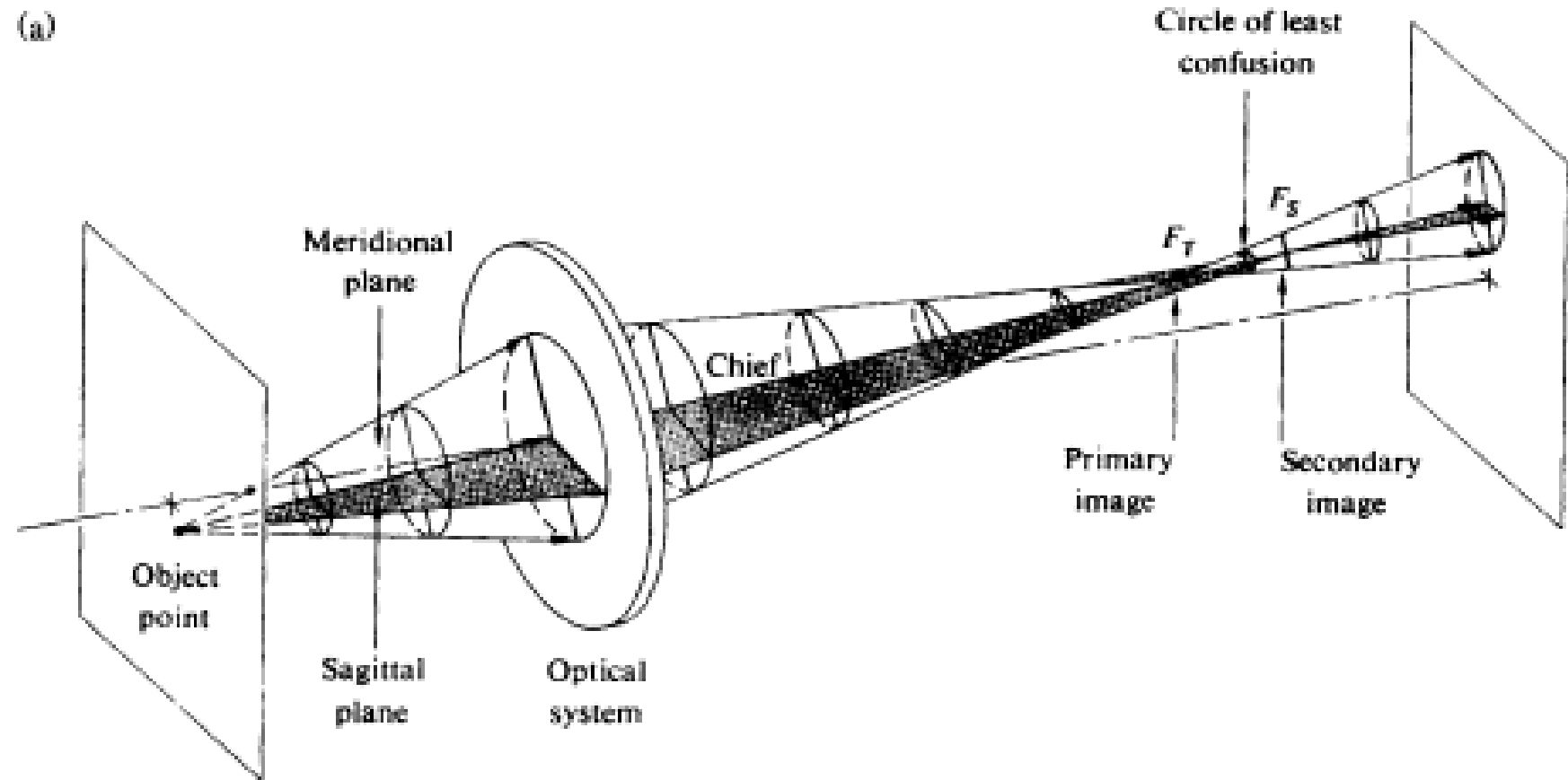
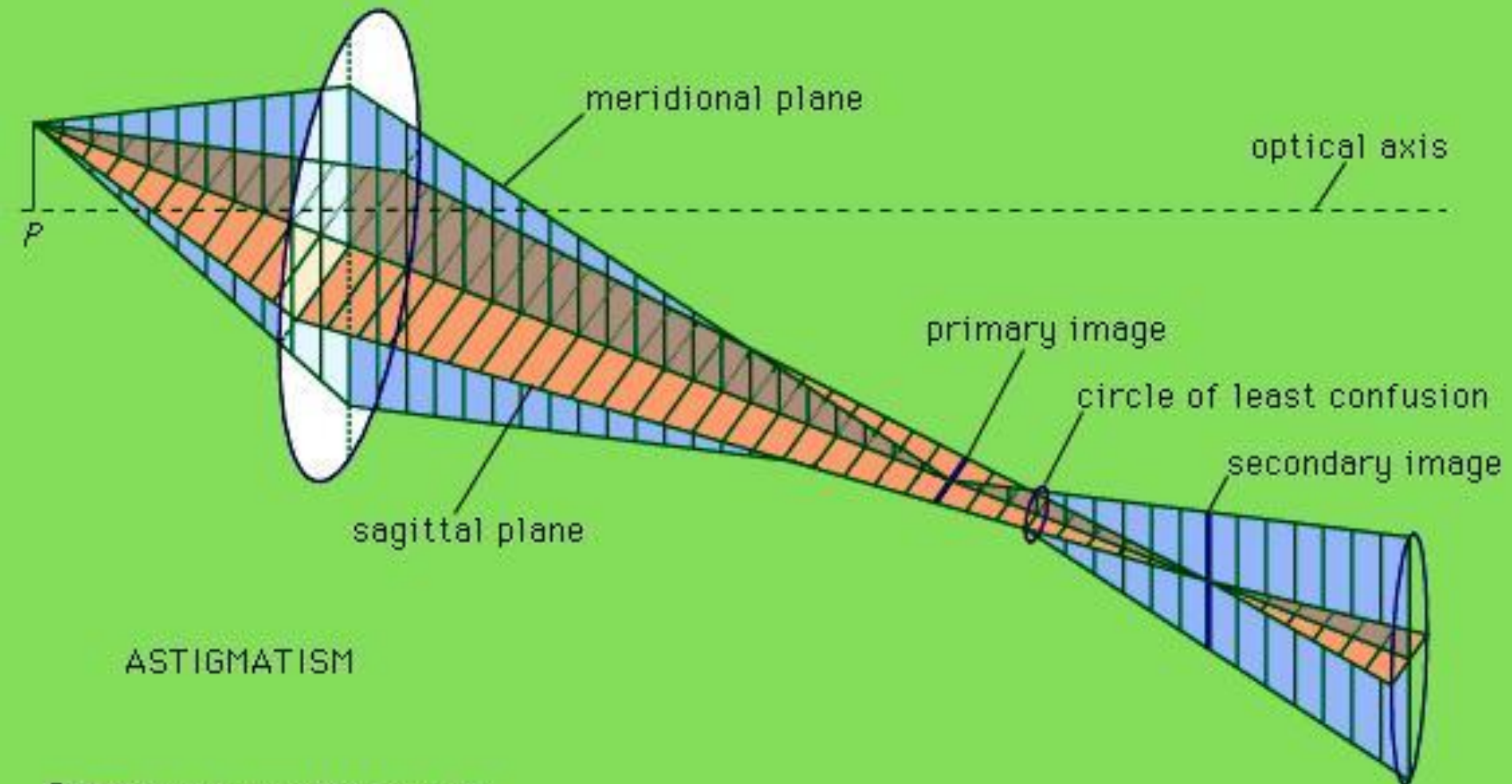


Figure 6.25 The effect of stop location on coma.

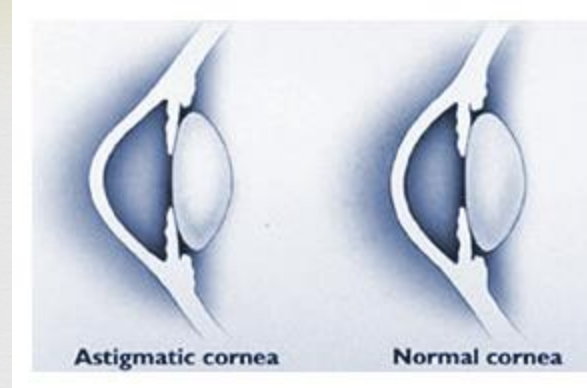
Astigmatism



Astigmatism



Astigmatism



Astigmatism causes blur along one direction

ABCD

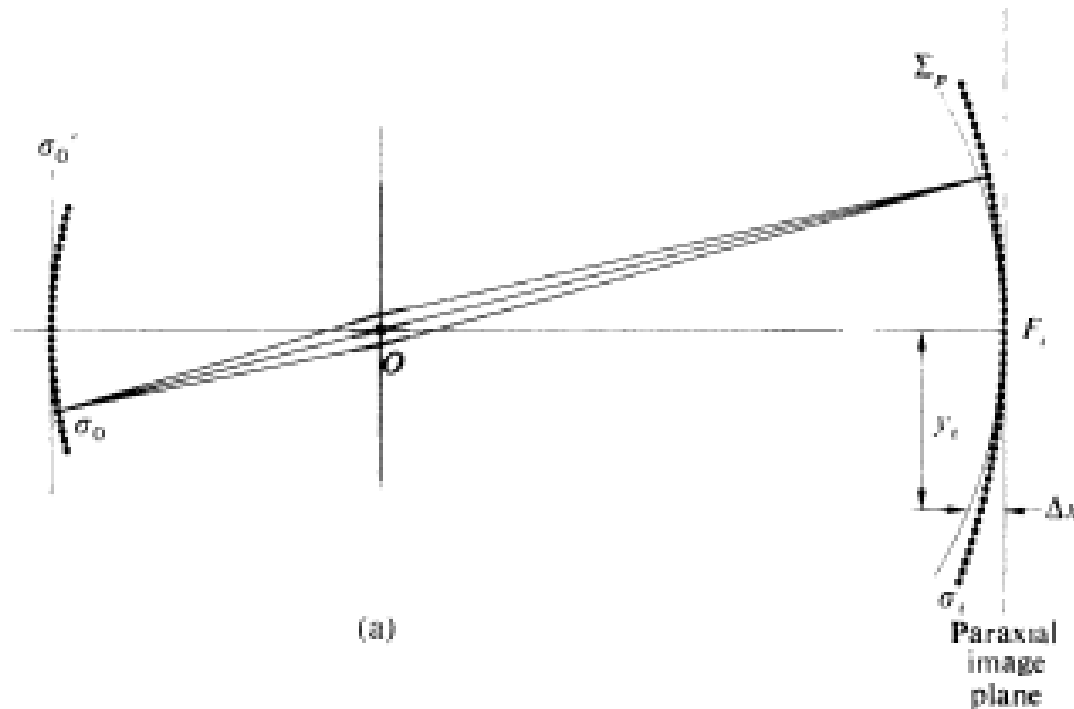
Vertical lines may be more blurred

ABCD

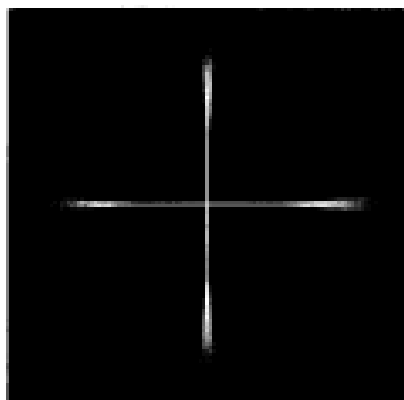
Horizontal lines can be more blurred



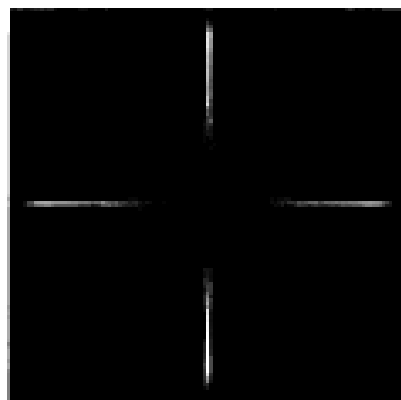
Field Curvature



(b)

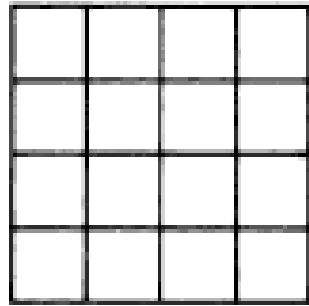


(c)

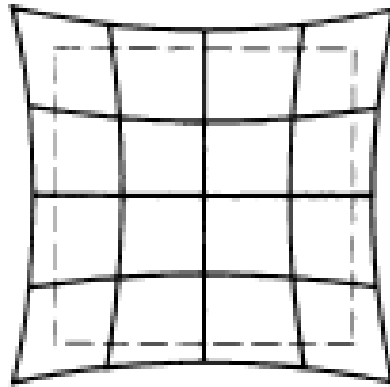


$$\Delta x = \frac{y_i^2}{2} \sum_{j=1}^m \frac{1}{n_j f_j}$$

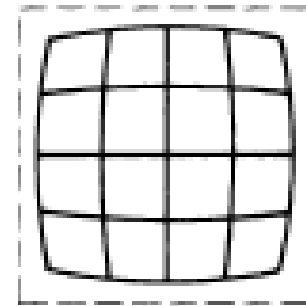
Distortion



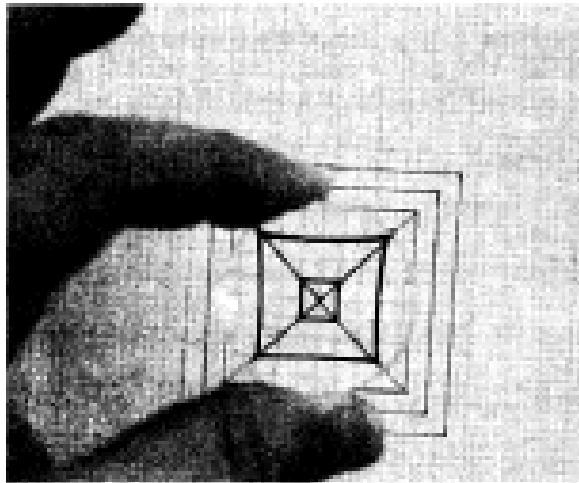
(a)



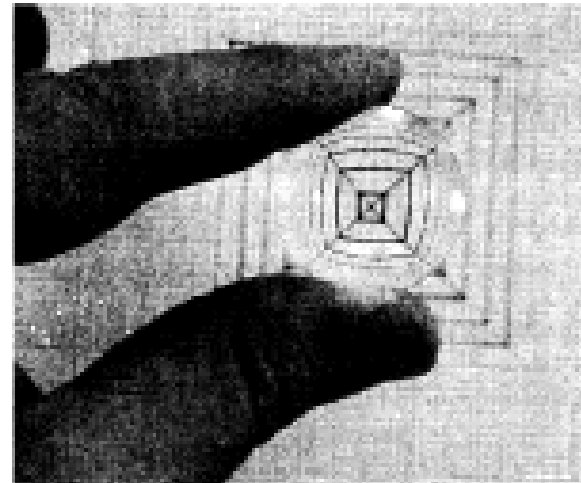
(b)



(c)

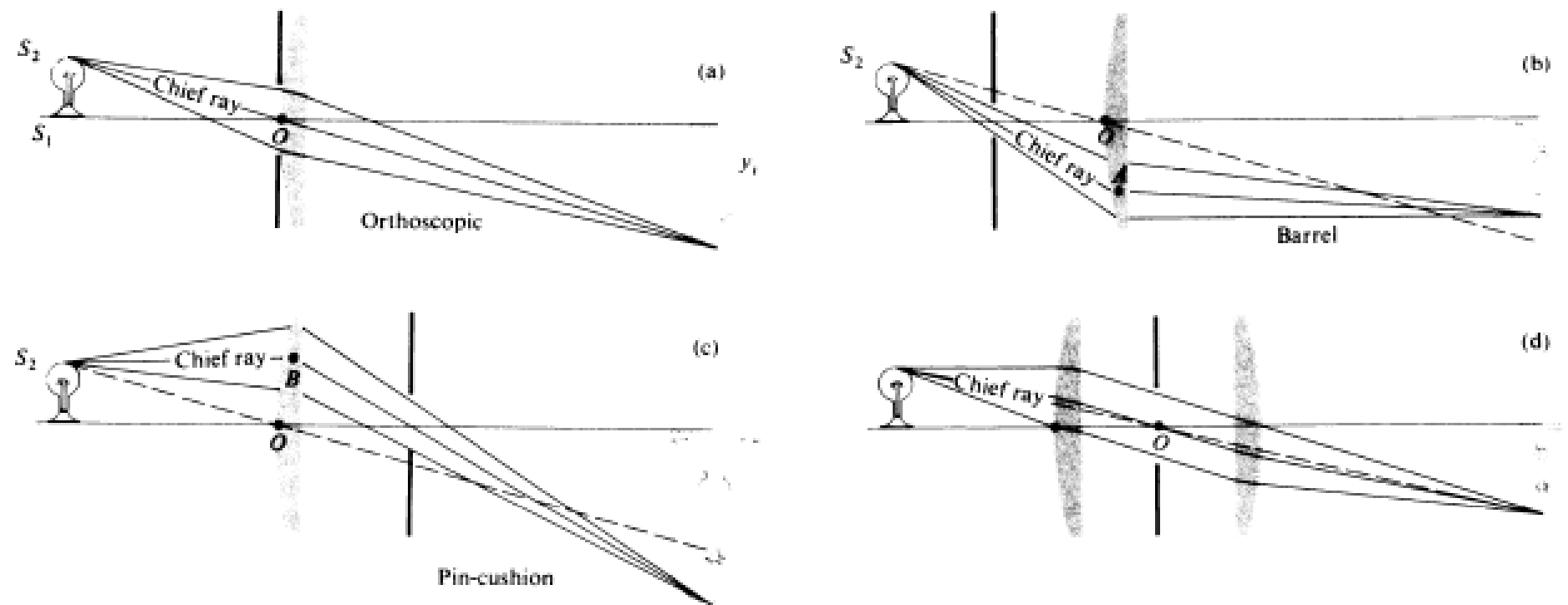


(d)



(e)

The Effect of Stop Location

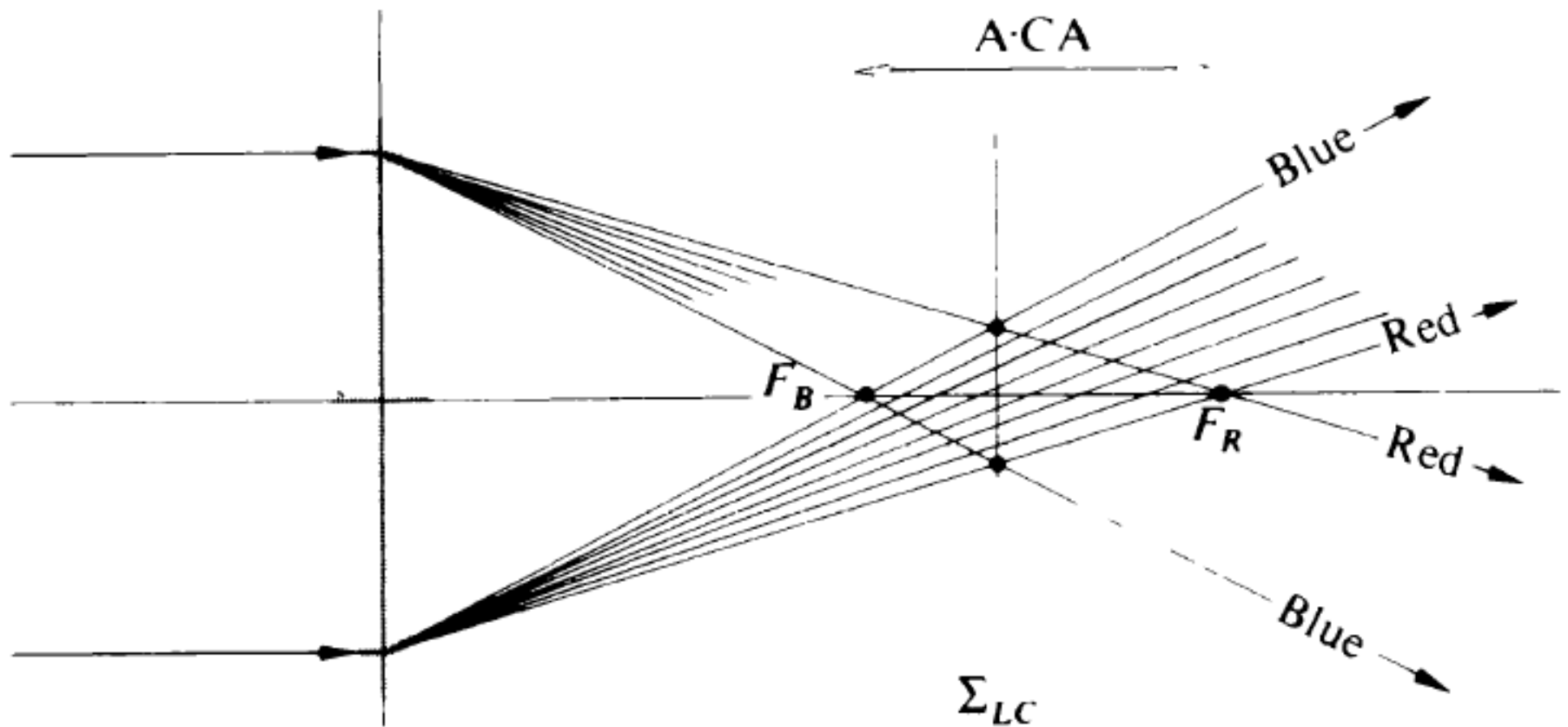


Chromatic Aberrations

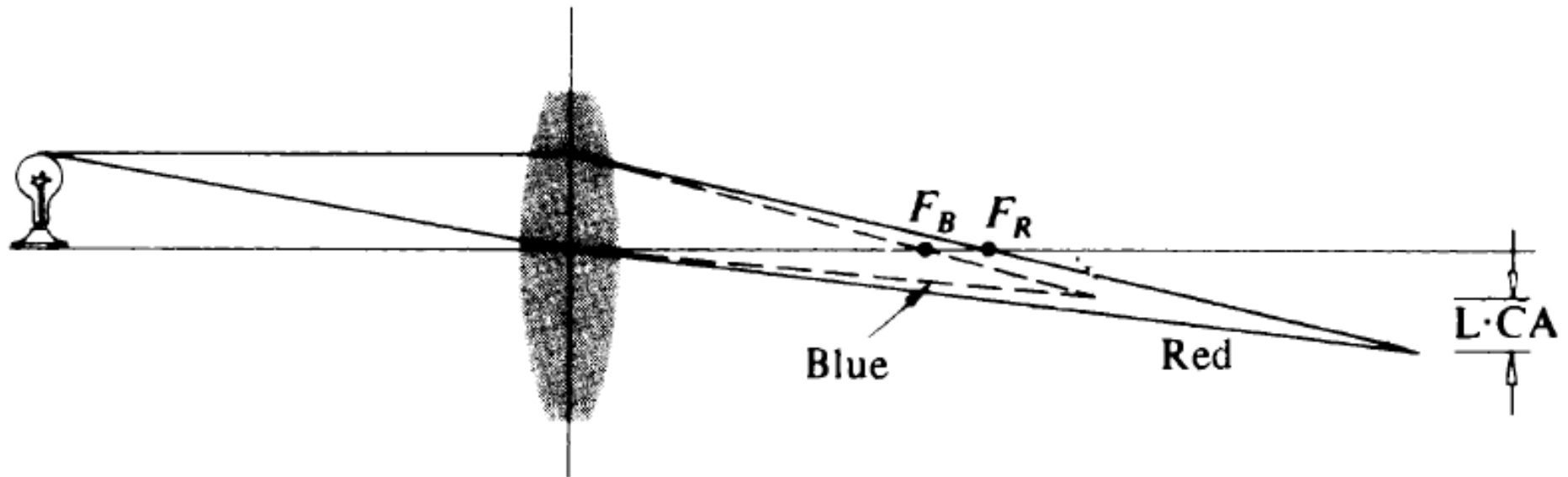


$$\frac{1}{f} = (n_l - 1) \left(\frac{1}{R_1} - \frac{1}{R_2} \right) \quad [5.16]$$

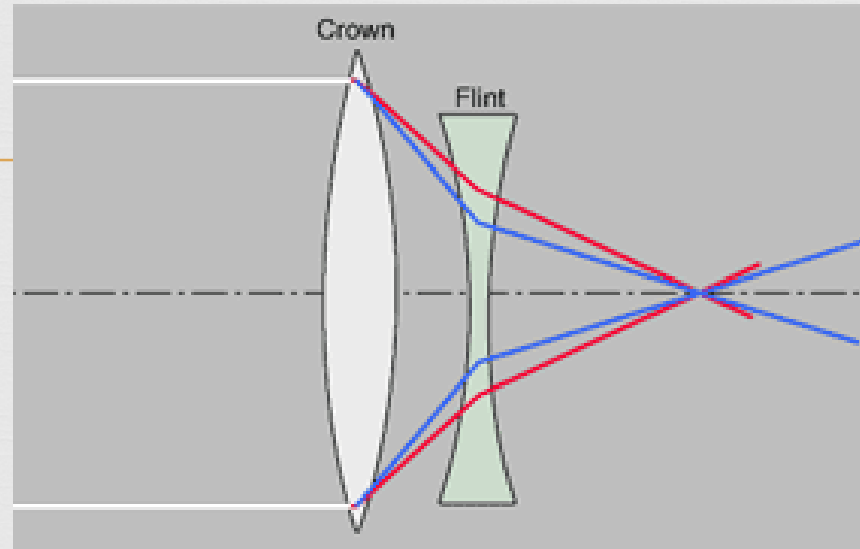
Axial Chromatic Aberration



Lateral Chromatic Aberration



Achromatic Doublet



6.4 Grin Systems

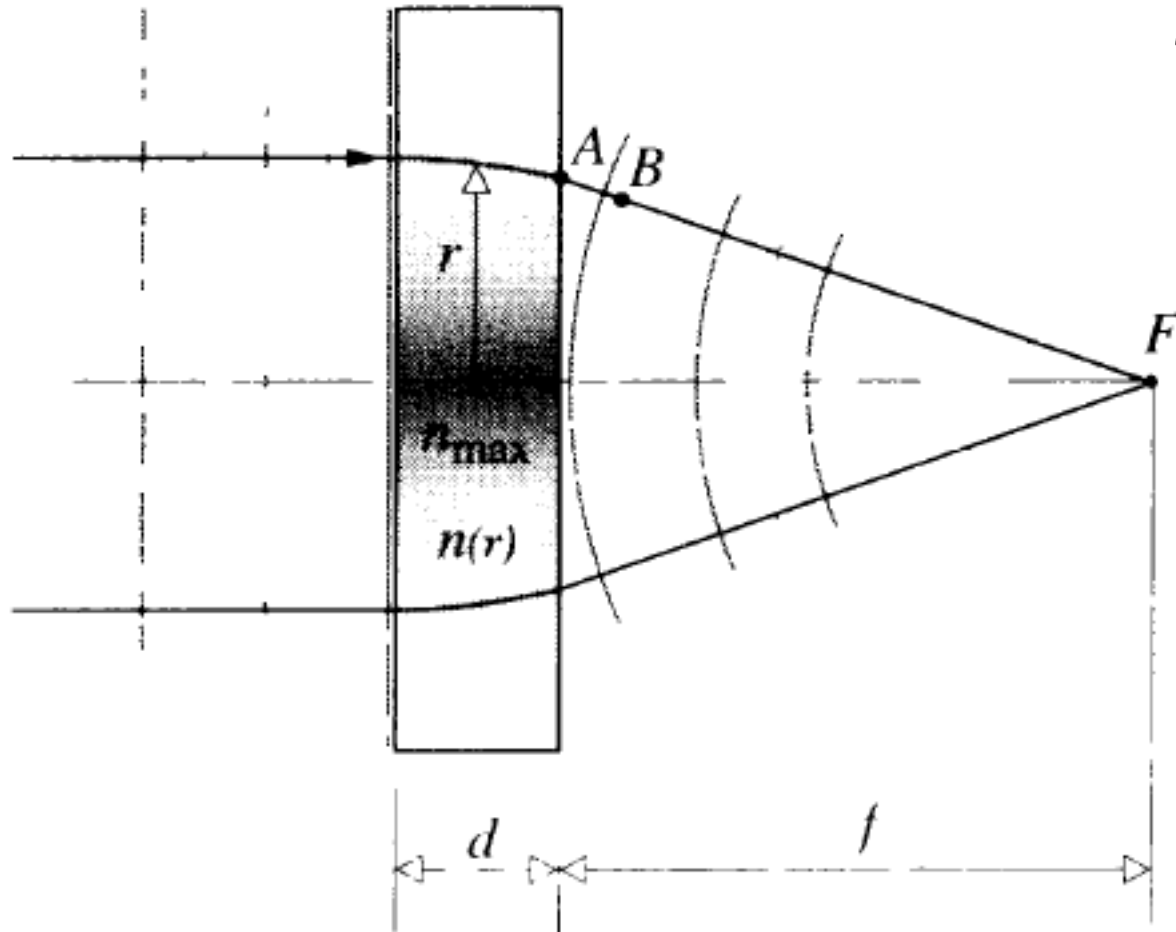
$$(OPL)_r + \overline{AB} = (OPL)_o$$

and

$$n(r)d + \overline{AB} = n_{\max}d$$

But $\overline{AF} \approx \sqrt{r^2 + f^2}$; moreover, $\overline{AB} = \overline{AF} - f$ and so

$$n(r) = n_{\max} - \frac{\sqrt{r^2 + f^2} - f}{d}$$



$$n(r) = n_{\max} - \frac{r^2}{2fd}$$

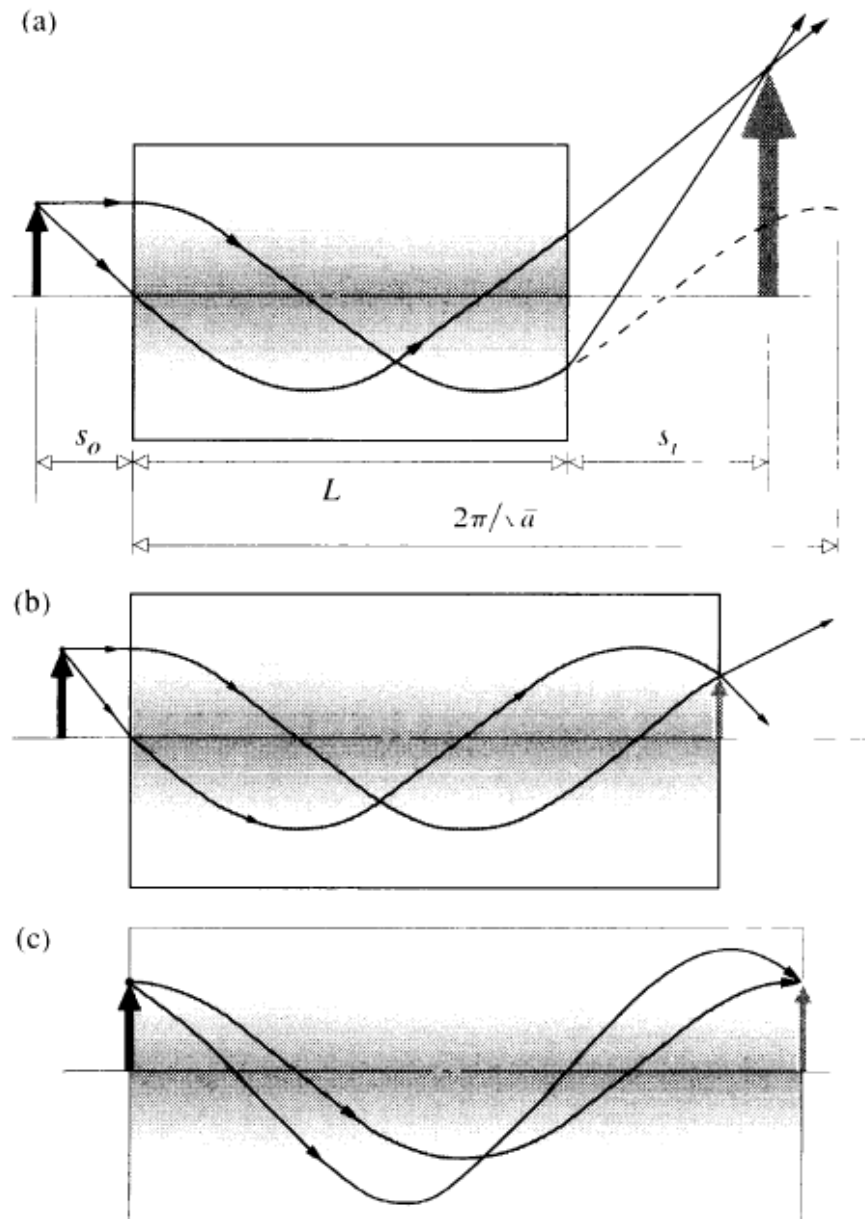


Figure 6.43 (a) A radial-GRIN rod producing a real, magnified, erect image. (b) Here the image is formed on the face of the rod. (c) This is a convenient setup for use in a copy machine.

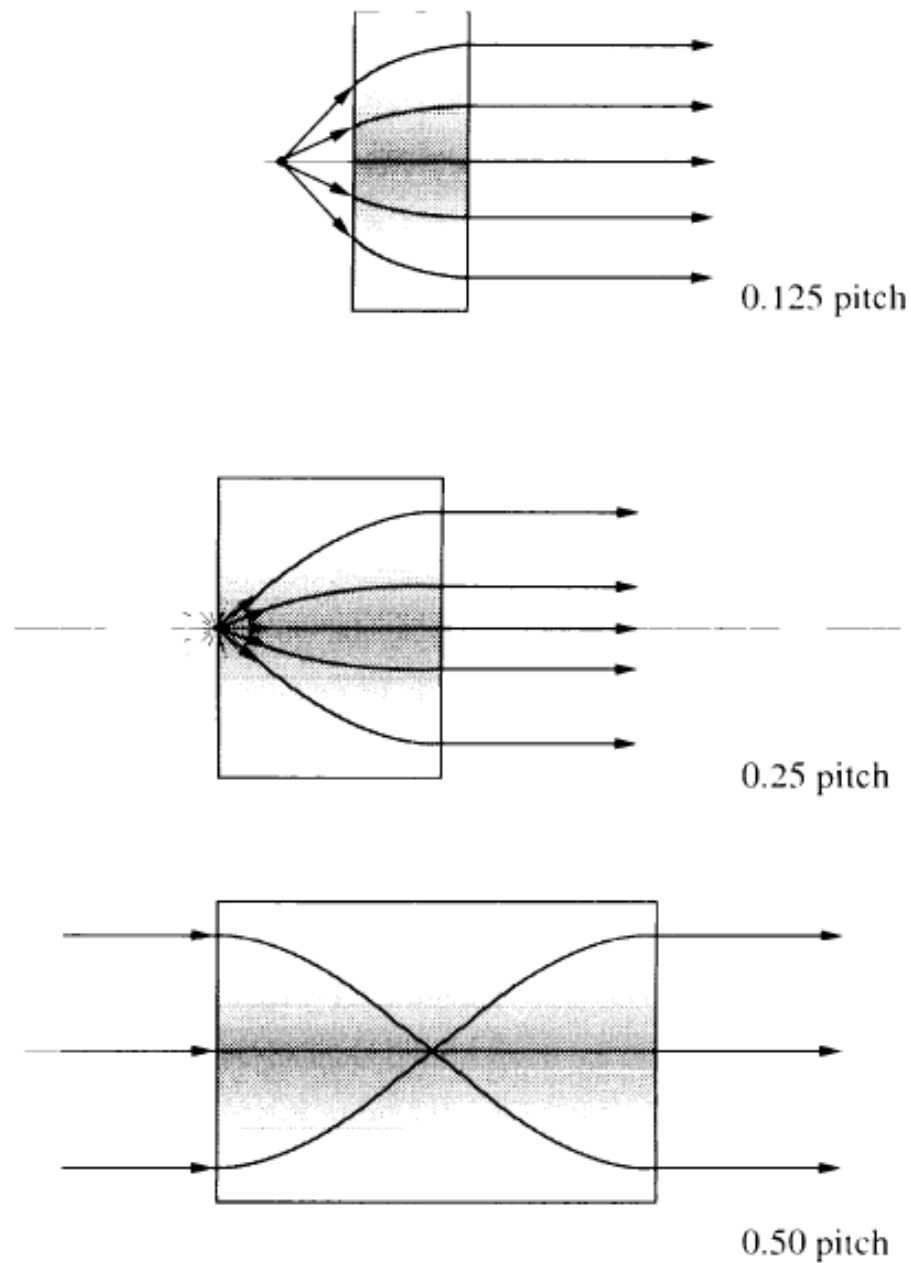


Figure 6.44 Radial GRIN lenses with several pitches used in a few typical ways.