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## PHYS 3033 - Electricity and Magnetism I

### Quiz 8

Time allowed: 15 minutes

3 Nov 2015

A steady current  $I$  flows down a long cylindrical wire of radius  $a$  (Fig. 1). Find the magnetic field, both inside and outside the wire, if

- (a) The current is uniformly distributed over the outside surface of the wire.
- (b) The current distributed in such a way that  $J$  is proportional to  $s$ , the distance from the axis.

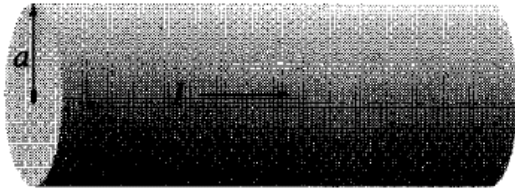


Fig. 1

### Solution

$$(a) \quad \oint \mathbf{B} \cdot d\mathbf{l} = B2\pi s = \mu_0 I_{enc} \Rightarrow \mathbf{B} = \begin{cases} 0, & \text{for } s < a \\ \frac{\mu_0 I}{2\pi s} \hat{\phi}, & \text{for } s > a \end{cases}.$$

$$(b) \quad J = ks; I = \int_0^a J da = \int_0^a ks(2\pi s) ds = \frac{2\pi ka^3}{3} \Rightarrow k = \frac{3I}{2\pi a^3}.$$

$$I_{enc} = \int_0^s J da = \int_0^s k\bar{s}(2\pi\bar{s}) d\bar{s} = I = \frac{2\pi ks^3}{3} = I \frac{s^3}{a^3}, \text{ for } s < a; I_{enc} = I, \text{ for } s > a.$$

So

$$\mathbf{B} = \begin{cases} \frac{\mu_0 Is^2}{2\pi a^3} \hat{\phi}, & \text{for } s < a \\ \frac{\mu_0 I}{2\pi s} \hat{\phi}, & \text{for } s > a \end{cases}.$$