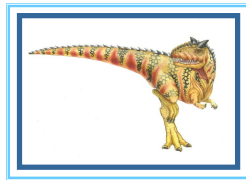


# Chapter 9: Virtual-Memory Management



## Objectives

- To describe the benefits of a virtual memory system
- To explain the concepts of demand paging, page-replacement algorithms, and allocation of page frames
- To discuss the principle of the working-set model



## Chapter 9: Virtual-Memory Management

- Background
- Demand Paging
- Page Replacement
- Allocation of Frames
- Thrashing
- Other Considerations



## Background

- Code needs to be in memory to execute, but entire program is not needed in many cases.
  - Error code, unusual routines. Some errors seldom, if ever, occur in practice, this code is almost never executed
  - large data structures such as arrays, lists and tables are often allocated more memory than they actually need. For example, an array may be declared 100x100 elements, even though it is seldom larger than 10x10
- Consider ability to execute partially-loaded program
  - Program no longer constrained by limits of physical memory. Programs can be written with an extremely large virtual memory address, simplifying the programming task
  - Each user program could take less physical memory, more programs could be run at the same time, which increases CPU utilization (degree of multiprogramming) and throughput
  - Less I/O would be needed to load or swap user programs into physical memory, so each user program would run faster.



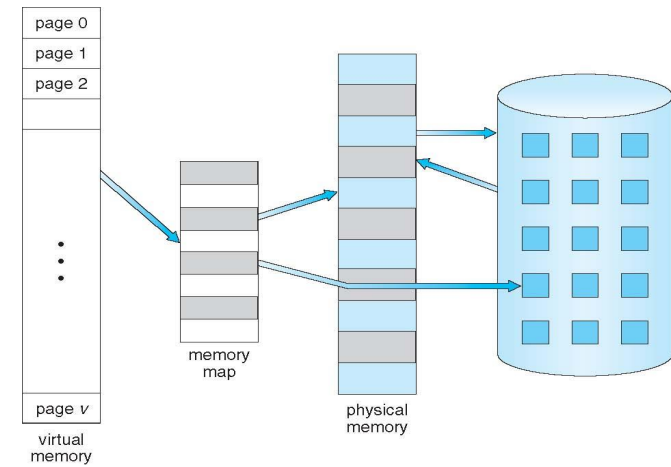


## Background

- **Virtual memory** – separation of user logical memory from physical memory
  - Only part of the program needs to be in memory for execution
  - Logical address space can therefore be much larger than physical address space
  - Allows address spaces to be shared by several processes. For instance, system libraries can be shared by several processes
  - Allows for more efficient process creation, as pages can be shared during process creation, thus speeding up the process creation
  - More programs running concurrently
  - Less I/O needed to load or swap processes
- Virtual memory can be implemented via:
  - Demand paging
  - Demand segmentation

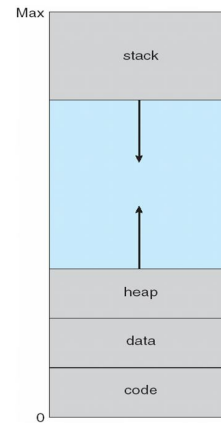


## Virtual Memory That is Larger Than Physical Memory

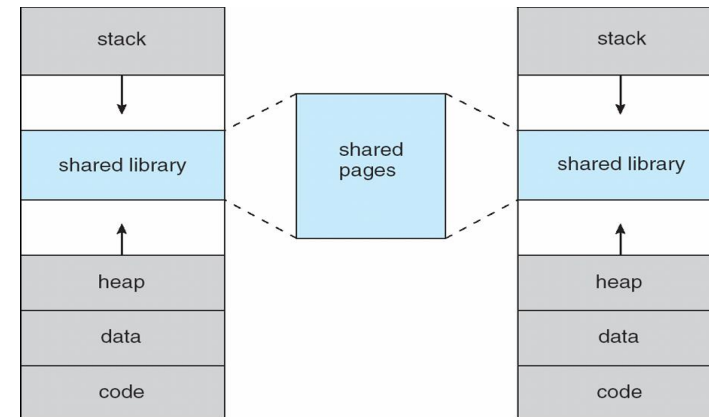


## Virtual-address Space

- Heap can grow upward in memory as it used in dynamic memory allocation
- Stack can grow downward in memory through successive function calls
- The large blank space (or hole) between the heap and stack is part of the virtual address space, but will require actual physical pages (space) only if the heap or stack grows.



## Shared Library Using Virtual Memory



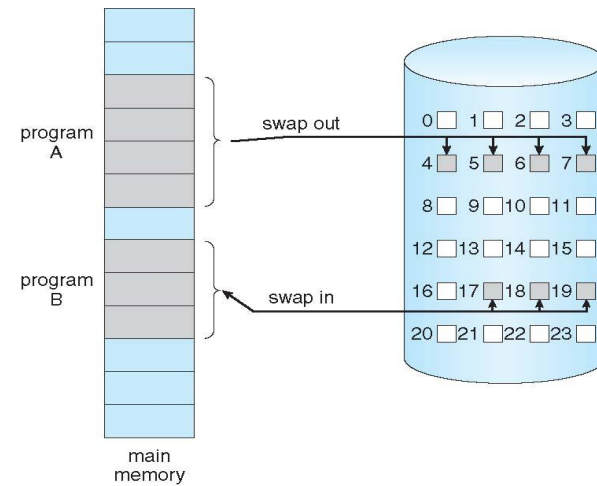


## Demand Paging

- Could bring entire process into memory at load time
- Or bring a page into memory only when it is needed
  - Less I/O needed, no unnecessary I/O
  - Less memory needed
  - Faster response
  - More users to be run
- Page is needed  $\Rightarrow$  reference to it
  - invalid reference  $\Rightarrow$  abort
  - not-in-memory  $\Rightarrow$  bring to memory
- **Lazy swapper** – never swaps a page into memory unless the page will be needed/referenced
  - Swapper that deals with pages is a **pager**, since a swapper manipulates entire processes, whereas a pager is concerned with the individual pages of a process.



## Transfer of a Paged Memory to Contiguous Disk Space



## Valid-Invalid Bit

- With each page table entry a valid-invalid bit is associated (**v**  $\Rightarrow$  in-memory – **memory resident**, **i**  $\Rightarrow$  not-in-memory)
- Initially valid-invalid bit is set to **i** on all entries
- Example of a page table snapshot:

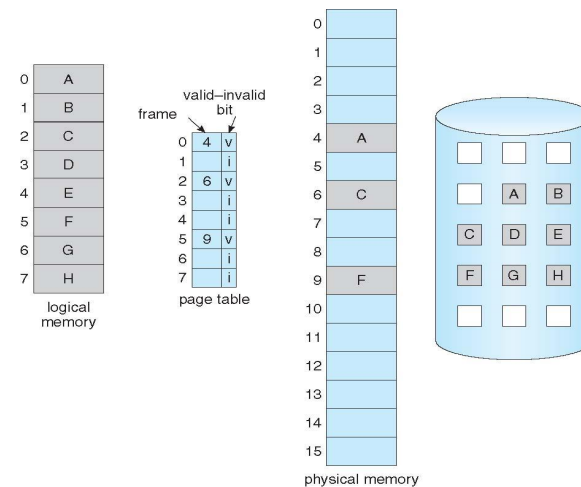
Frame #	valid-invalid bit
	v
	v
	v
	v
	i
....	
	i
	i

page table

- During address translation, if valid-invalid bit in page table entry is **i**  $\Rightarrow$  page fault



## Page Table When Some Pages Are Not in Main Memory





## Page Fault

- If there is a reference to a page, first reference to that page will trap to operating system:
  - page fault

  1. Operating system looks at another table to decide:
    - Invalid reference  $\Rightarrow$  abort
    - Just not in memory
  2. Get empty frame
  3. Swap page into frame via scheduled disk operation
  4. Reset tables to indicate page now in memory  
Set validation bit =  $\checkmark$
  5. Restart the instruction that caused the page fault

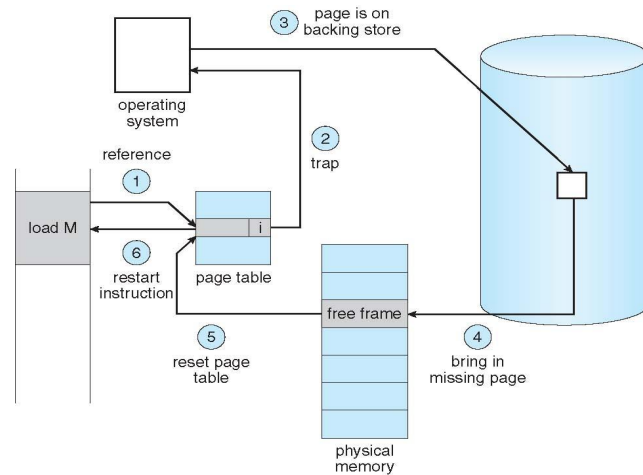


## Aspects of Demand Paging

- Extreme case – start process with *no* pages in memory
  - OS sets instruction pointer to first instruction of process, non-memory-resident  $\rightarrow$  page fault
  - And for every other process pages on first access
  - **Pure demand paging**
- Actually, a given instruction could access multiple pages  $\rightarrow$  multiple page faults
  - Pain decreased because of **locality of reference**
- Hardware support is needed for demand paging
  - Page table with valid / invalid bit
  - Secondary memory (swap device with **swap space**)
  - Instruction restart



## Steps in Handling a Page Fault



## Performance of Demand Paging

- Stages in Demand Paging

  1. Trap to the operating system
  2. Save the user registers and process state
  3. Determine that the interrupt was a page fault
  4. Check that the page reference was legal and determine the location of the page on the disk
  5. Issue a read from the disk to a free frame in physical memory:
    1. Wait in a queue for this device until the read request is serviced
    2. Wait for the device seek and/or latency time
    3. Begin the transfer of the page to a free frame
  6. While waiting, allocate the CPU to some other user(s)
  7. Receive an interrupt from the disk I/O subsystem (I/O completed)
  8. Save the registers and process state for the other user
  9. Determine that the interrupt was from the disk
  10. Correct the page table and other tables to show page is now in memory
  11. Wait for the CPU to be allocated to this process again
  12. Restore the user registers, process state, and new page table, and then resume the interrupted instruction





## Performance of Demand Paging (Cont.)

- Page Fault Rate  $0 \leq p \leq 1$ 
  - if  $p = 0$  no page faults
  - if  $p = 1$ , every reference is a fault

- Effective Access Time (EAT)

$$\begin{aligned} \text{EAT} = & (1 - p) \times \text{memory access} \\ & + p (\text{page fault overhead} \\ & \quad + \text{swap page out} \\ & \quad + \text{swap page in} \\ & \quad + \text{restart overhead} \\ & ) \end{aligned}$$



## Demand Paging Example

- Memory access time = 200 nanoseconds
- Average page-fault service time = 8 milliseconds
- $\text{EAT} = (1 - p) \times 200 + p (8 \text{ milliseconds})$   
 $= (1 - p) \times 200 + p \times 8,000,000$   
 $= 200 + p \times 7,999,800$
- If one access out of 1,000 causes a page fault, then  
 $\text{EAT} = 8.2 \text{ microseconds.}$   
 This is a slowdown by a factor of 40!!
- If want performance degradation < 10 percent
  - $220 > 200 + 7,999,800 \times p$
  - $20 > 7,999,800 \times p$
  - $p < .0000025$
  - < one page fault in every 400,000 memory accesses



## What Happens if There is no Free Frame?

- Used up by process pages
- Also in demand from the kernel, I/O buffers, etc.
- How much to allocate to each?
- Page replacement – find some page in memory, but not really in use, page it out
  - Algorithm – terminate? swap out? replace the page?
  - Performance – want an algorithm which will result in the minimum number of page faults
- Same page may be brought into memory several times



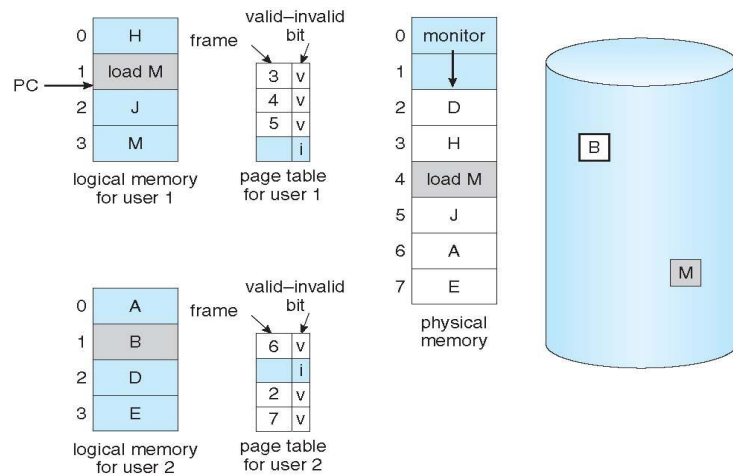
## Page Replacement

- Prevent over-allocation of memory by modifying page-fault service routine to include page replacement
- Use **modify (dirty) bit** to reduce overhead of page transfers – only modified pages are written back to disk
- Page replacement completes separation between logical memory and physical memory – large virtual memory can be supported on a smaller physical memory





## Need For Page Replacement



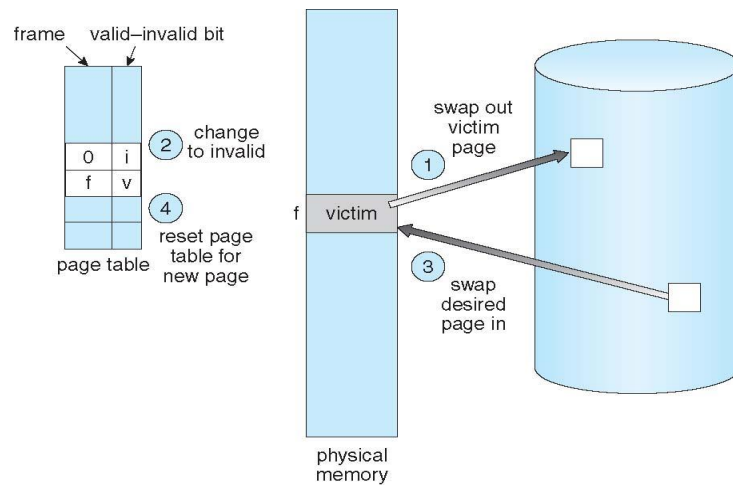
## Basic Page Replacement

1. Find the location of the desired page on disk
2. Find a free frame:
  - If there is a free frame, use it
  - If there is no free frame, use a page replacement algorithm to select a **victim frame**
  - Write victim frame to disk if dirty
3. Bring the desired page into the (newly) free frame; update the page and frame tables
4. Continue the process by restarting the instruction that caused the trap

Note now potentially 2 page transfers for page fault – increasing EAT



## Page Replacement



## Page and Frame Replacement Algorithms

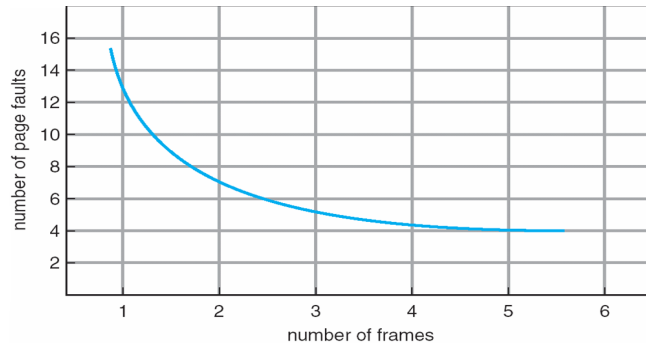
- **Frame-allocation algorithm** determines
  - How many frames to give each process
  - Which frames to replace
- **Page-replacement algorithm**
  - Want the lowest page-fault rate on both first access and re-access
- Evaluate algorithm by running it on a particular string of memory references (reference string) and computing the number of page faults on that string
  - String is just page numbers, not full addresses
  - Repeated access to the same page does not cause a page fault (thus does not show)

■ In all our examples, the reference string is

**7,0,1,2,0,3,0,4,2,3,0,3,0,3,2,1,2,0,1,7,0,1**



## Graph of Page Faults Versus The Number of Frames



## First-In-First-Out (FIFO) Algorithm

- Reference string: 7,0,1,2,0,3,0,4,2,3,0,3,0,3,2,1,2,0,1,7,0,1
- 3 frames (3 pages can be in memory at a time per process)

1	7	2	4	0	7
2	0	3	2	1	0
3	1	0	3	2	1

15 page faults

- Can vary by reference string: consider 1,2,3,4,1,2,5,1,2,3,4,5
  - Adding more frames can cause more page faults!
    - Belady's Anomaly
- How to track ages of pages?
  - Just use a FIFO queue



## FIFO Page Replacement

reference string

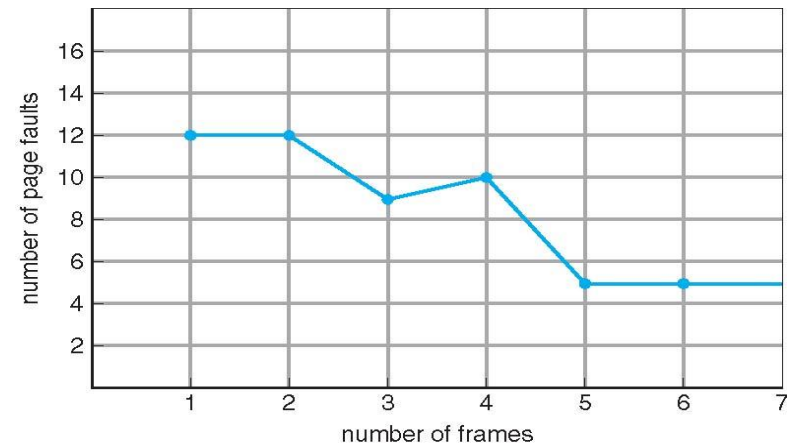
7 0 1 2 0 3 0 4 2 3 0 3 2 1 2 0 1 7 0 1

7	7	7	2	2	2	4	4	4	0	0	0	0	0	0	0	7	7	7
	0	0	0	3	3	3	2	2	2	1	1	1	1	1	1	1	0	0
		1	1	1	0	0	0	0	3	3	3	3	3	3	3	2	2	2

page frames



## FIFO Illustrating Belady's Anomaly





## The Optimal Algorithm (OPT)

- Replace page that will not be used for longest period of time
  - 9 is the optimal for the example on the next slide
- How do you know this?
  - Can't read the future
- Used for measuring how well your algorithm performs



## Optimal Page Replacement

reference string

7 0 1 2 0 3 0 4 2 3 0 3 2 1 2 0 1 7 0 1

7	7	7	2	2	2	2	2	7
	0	0	0	0	4	0	0	0
		1	1	3	3	3	1	1

page frames



## Least Recently Used (LRU) Algorithm

- Use past knowledge rather than future
- Replace page that has not been used in the most amount of time
- Associate time of last use with each page

reference string

7 0 1 2 0 3 0 4 2 3 0 3 2 1 2 0 1 7 0 1

7	7	7	2	2	4	4	4	0	1	1	1
	0	0	0	0	0	0	3	3	3	0	0
		1	1	3	3	2	2	2	2	2	7

page frames

- 12 faults – better than FIFO but worse than OPT
- Generally good algorithm and frequently used
- But how to implement?



## LRU Algorithm (Cont.)

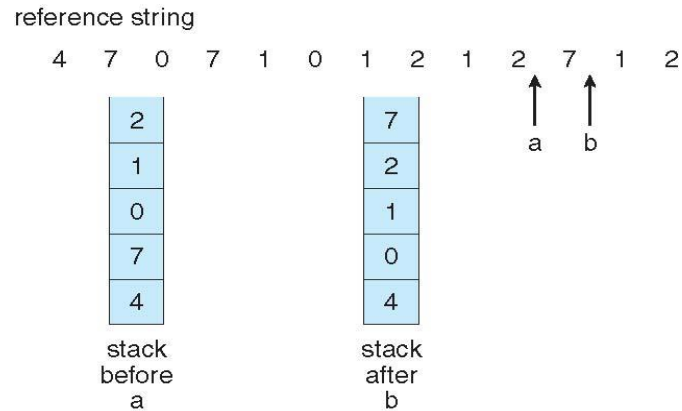
- Counter implementation
  - Every page entry has a counter; every time page is referenced through this entry, copy the clock into the counter
  - When a page needs to be changed, look at the counters to find the smallest value
    - Search through table needed
- Stack implementation
  - Keep a stack of page numbers in a double link form:
    - Page referenced:
      - move it to the top
      - requires 6 pointers to be changed
    - But each update more expensive
    - No need to search for replacement
- LRU and OPT are cases of **stack algorithms** that don't have Belady's Anomaly
  - A **stack algorithm** is an algorithm for which it can be shown (or proved) that the set of pages in memory for n frames is always a **subset** of the set of pages that would be in memory with n+1 frames.







## Use Of A Stack To Record The Most Recent Page References

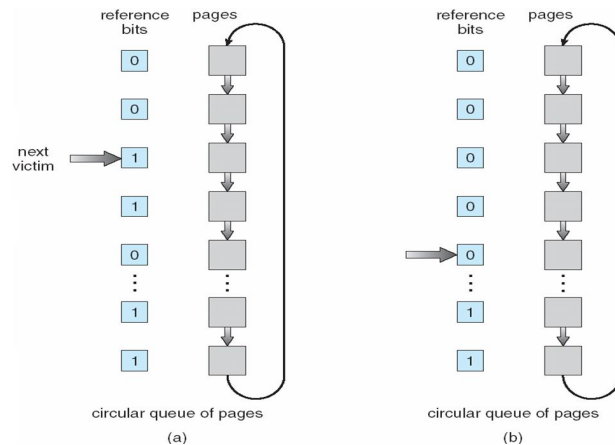


## LRU Approximation Algorithms

- LRU needs special hardware and still slow
- **Reference bit**
  - With each page associate a bit, initially = 0
  - When page is referenced bit set to 1
  - Replace any with reference bit = 0 (if one exists)
    - ▶ We do not know the order, however
- **Second-chance algorithm**
  - Generally FIFO, plus hardware-provided reference bit
  - Clock replacement
  - If page to be replaced has
    - ▶ Reference bit = 0 -> replace it
    - ▶ reference bit = 1 then:
      - set reference bit 0, leave page in memory
      - replace next page, subject to same rules (FIFO and clock)



## Second-Chance (Clock) Page-Replacement Algorithm



## Counting Algorithms

- Keep a counter of the number of references that have been made to each page
  - Not commonly used
- The **least frequently used (LFU)** Algorithm: replaces the page with the smallest count/
- The **most frequently used (MFU)** Algorithm: replace the page with the largest count based on the argument that the page with the smallest count was probably just brought in and has yet to be used
- Neither LFU nor MFU replacement is commonly used. The implementation of such algorithms is expensive, and they do not approximate OPT replacement well





## Allocation of Frames

- Each process needs certain *minimum* number of frames in order to execute program
- Example: IBM 370 – 6 pages to handle SS MOVE instruction:
  - instruction is 6 bytes, might span 2 pages
  - 2 pages to handle *from*
  - 2 pages to handle *to*
- *The Maximum* of course is the total frames in the system
- Two major allocation schemes
  - fixed allocation
  - priority allocation
- Many variations



## Fixed Allocation

- Equal allocation – For example, if there are 100 frames (after allocating frames for the OS) and 5 processes, give each process 20 frames
- Proportional allocation – Allocate according to the size of process
  - Dynamic as the degree of multiprogramming, process sizes change over the time

$$\begin{array}{l}
 - s_i = \text{size of process } p_i \\
 - S = \sum s_i \\
 - m = \text{total number of frames} \\
 - a_i = \text{allocation for } p_i = \frac{s_i}{S} \times m
 \end{array}
 \qquad
 \begin{array}{l}
 m = 64 \\
 s_1 = 10 \\
 s_2 = 127 \\
 a_1 = \frac{10}{137} \times 64 \approx 5 \\
 a_2 = \frac{127}{137} \times 64 \approx 59
 \end{array}$$



## Priority Allocation

- Use a proportional allocation scheme using priorities rather than size
- If process  $P_i$  generates a page fault,
  - select for replacement one of its frames
  - select for replacement a frame from a process with lower priority number



## Global vs. Local Allocation

- **Global replacement** – process selects a replacement frame from the set of all frames, even if that frame is currently allocated to some other process; thus, one process can take a frame from another
  - This can result in better system throughput
  - But then process execution time can vary greatly, as a process cannot control its own page-fault rate.
- **Local replacement** – each process selects from only its own set of allocated frames
  - More consistent per-process performance
  - But possibly underutilized memory, since pages allocated to a process can not be utilized by another process, even if this page is not currently used by the process holding it



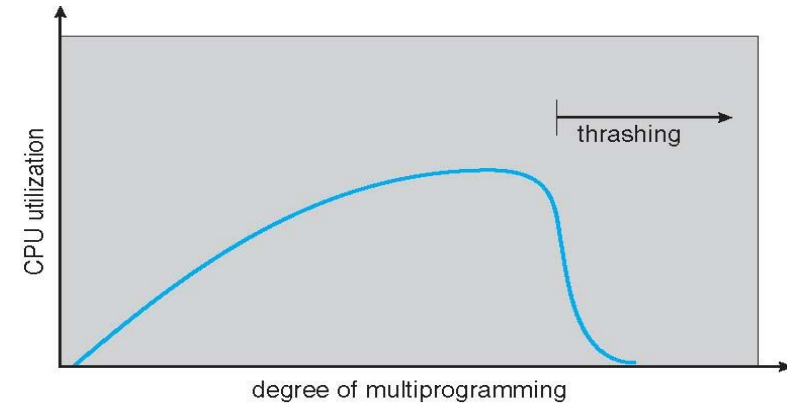


## Thrashing

- If a process does not have “enough” pages, the page-fault rate is very high
  - Page fault to get page
  - Replace existing frame
  - But quickly need replaced frame back
  - This leads to:
    - ▶ Low CPU utilization
    - ▶ Operating system thinking that it needs to increase the degree of multiprogramming
    - ▶ Another process added to the system – aggravate the problem
- **Thrashing** ≡ a process is busy swapping pages in and out



## Thrashing (Cont.)

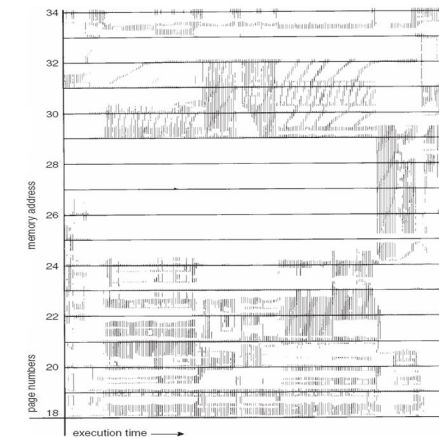


## Demand Paging and Thrashing

- Why does demand paging work?
  - **Locality model**
    - Process migrates from one locality to another
    - Localities may overlap
- Why does thrashing occur?
  - $\Sigma$  size of locality > total memory size
    - We can limit effects by using local or priority page replacement, as thrashing in one process can not steal frames from another process and cause the latter to thrash as well



## Locality In A Memory-Reference Pattern





## Working-Set Model

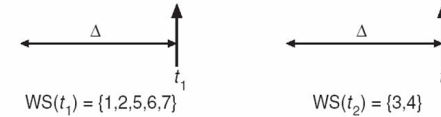
- $\Delta$   $\equiv$  working-set window  $\equiv$  a fixed number of page references  
Example: 10,000 instructions
- $WSS_i$  (working set of Process  $P_i$ ) = total number of pages referenced in the most recent  $\Delta$  (varies in time)
  - if  $\Delta$  too small will not encompass entire locality
  - if  $\Delta$  too large will encompass several localities
  - if  $\Delta = \infty \Rightarrow$  will encompass entire program
- $D = \sum WSS_i \equiv$  total demand frames
  - Approximation of the current locality in the system (of all processes)
- if  $D > m \Rightarrow$  Thrashing – at least one process is short of memory
- Policy if  $D > m$ , then suspend or swap out one of the processes
- The working-set strategy prevent thrashing while keeping the degree of multiprogramming as high as possible, thus optimizes CPU utilization



## Working-set model

page reference table

... 2 6 1 5 7 7 7 7 5 1 6 2 3 4 1 2 3 4 4 4 3 4 3 4 4 4 1 3 2 3 4 4 4 4 3 4 4 4 ...



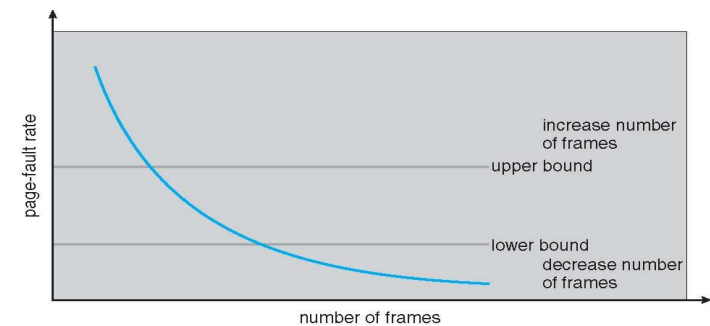
## Keeping Track of the Working Set

- It is difficult to keep track of the working set, as working-set window is a moving window which needs to be updated for each memory reference
- Approximate with interval timer + a reference bit
- Example:  $\Delta = 10,000$ 
  - Timer interrupts after every 5000 time units
  - Keep in memory 2 bits for each page
  - Whenever a timer interrupts copy and sets the values of all reference bits to 0
  - If one of the bits in memory = 1  $\Rightarrow$  page in working set
- This is not completely accurate, as we cannot tell where, within an interval of 5,000, a reference occurred
- Improvement = 10 bits and interrupt every 1000 time units, more accurate but cost is higher



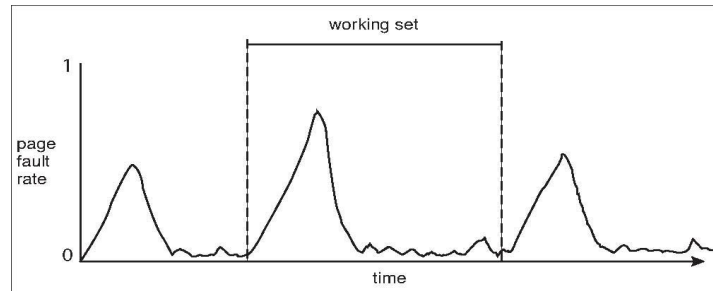
## Page-Fault Frequency

- More direct approach than WSS
- Establish "acceptable" **page-fault frequency** rate and use local replacement policy
  - If actual rate too low, process loses frame
  - If actual rate too high, process gains frame





## Working Sets and Page Fault Rates



## Other Considerations -- Prepaging

### Prepaging

- To reduce the large number of page faults that occurs at process startup
- Prepage all or some of the pages a process will need, before they are referenced
- But if prepagged pages are unused, I/O and memory was wasted
- Assume  $s$  pages are prepagged and  $\alpha$  of the pages is used
  - Is cost of  $s * \alpha$  save pages faults  $>$  or  $<$  than the cost of prepagging  $s * (1 - \alpha)$  unnecessary pages?
  - $\alpha$  near zero  $\Rightarrow$  prepagging loses



## Other Issues – Page Size

- Sometimes OS designers have a choice
  - Especially if running on custom-built CPU
- Page size selection must take into consideration:
  - Fragmentation
  - Page table size
  - [Resolution](#)
  - I/O overhead
  - Number of page faults
  - Locality
  - TLB size and effectiveness
- Always power of 2, usually in the range  $2^{12}$  (4,096 bytes) to  $2^{22}$  (4,194,304 bytes)
- On average, growing over time



## Other Issues – TLB Reach

- TLB Reach - The amount of memory accessible from the TLB
- TLB Reach = (TLB Size) X (Page Size)
- Ideally, the working set of each process is stored in the TLB
  - Otherwise there is a high degree of page faults
- Increase the Page Size
  - This may lead to an increase in fragmentation as not all applications require a large page size
- Provide Multiple Page Sizes
  - This allows applications that require larger page sizes the opportunity to use them without an increase in fragmentation





## Other Issues – Program Structure

### ■ Program structure

- `Int[128,128] data;`
- Each row is stored in one page
- Program 1

```
for (j = 0; j < 128; j++)  
  for (i = 0; i < 128; i++)  
    data[i,j] = 0;
```

128 x 128 = 16,384 page faults

- Program 2

```
for (i = 0; i < 128; i++)  
  for (j = 0; j < 128; j++)  
    data[i,j] = 0;
```

128 page faults

