THE HONG KONG UNIVERSITY OF SCIENCE & TECHNOLOGY Computer Organization (COMP 2611)

Spring Semester, 2014

Final Examination

May 23, 2014

Name: ______

Student ID:_____

Email:

Lab Section Number:

Instructions:

- 1. This examination paper consists of 13 pages in total, including 7 questions within 11 pages, 2 appendices.
- 2. Please do NOT use pencils to answer the questions.
- 3. Please answer all the questions in the spaces provided on the examination paper.
- 4. Please read each question carefully, answer clearly and to the point. Make sure that your answers are neatly written.
- 5. Keep all pages stapled together. You can tear off the appendix only.
- 6. Calculator and electronic devices are not allowed.
- 7. The examination period will last for 2.5 hours.

Question	Percentage %	Score
1 Cache Performance	12	
2 Cache Architecture	15	
3 Single-cycle Datapath & Control	13	
4 Multi-cycle Datapath & Control	20	
5 MIPS Recursion	15	
6 MIPS Programming	10	
7 Pipeline	15	
TOTAL	100	

Question 1: Cache Performance (12 marks)

- a) The average memory access latency for a microprocessor with a single level cache is 2.4 clock cycles. If the data is present in the cache, it takes 1 clock cycle to fetch. Otherwise, (if data is not in the cache), 80 clock cycles are necessary to get it from the main memory. We want to improve the average memory access latency to 1.5 clock cycles by adding a 2nd level of cache on chip. This 2nd level of cache can be accessed in 6 clock cycles, and does not affect the first level cache access patterns and hit times, nor the access time to the main memory (i.e., 80 additional clock cycles).
 - 1. Give the general equation for the average memory access latency in a memory hierarchy with two-level cache, using the following notations: L1 Cache, hit time t₁, hit rate h₁; L2 Cache, hit time t₂, hit rate h₂; main memory access time t_{mem}. (2 marks)
 - 2. What is the expected hit rate in the 2nd level cache to achieve the target speedup (from 2.4 to 1.5 cycle)? Briefly show your calculation steps. (6 marks)

b) For a given machine, and a given program, if all the data and instructions could always be found in the first level cache, then on average the processor can finish an instruction within 2 clock cycles (i.e. the ideal CPI, CPI_{optimum} = 2).

However, measurements obtained show that the instruction miss rate is 12% and the data miss rate is 6%, and that on average, 30% of all instructions contain a data reference. The miss penalty for the cache is 10 cycles. What is the actual CPI for this program on this machine if we consider memory access overhead? (4 marks)

Question 2: Cache Architecture (15 marks)

 a) Consider a 16-way set associative cache of size 64K bytes. If a memory address is 32 bits and the block size is 64 bytes, answer the following questions. Briefly show your calculations. (5 marks)

Number of blocks in the cache =

Number of sets in the cache =

Number of bits for the byte offset =

Number of bits for the Index field =

Number of bits for the Tag field =

b) Given a 2-way set-associative cache with 3-bit tag, below is a sequence of memory accesses which are mapped to the same cache set. Assume the cache is initially empty. If LRU cache replacement strategy is used, fill in the blank below to indicate if a Hit or Miss happened to the each access. (5 marks)

	Tagf	Tag field of the memory accesses generated by CPU (from left to right):													
	101	101	100	111	011	100	011	011	100						
Hit/Miss	Miss	Hit													
	Cache Access Tracking:														
MRU	101	101													
LRU															



c) Consider the following 4-way set associative cache.

Complete the last two columns of the following table for the given sequence of memory accesses. (5 marks)

Address of the memory access generated by CPU	Assigned cache set	Hit or miss?
0000 1111 0101 0010 0011 0111 0100 0110		
0000 1111 0101 1010 0011 0111 0100 0110		
0000 1111 0101 0010 0011 0111 0111 1101		
0000 1111 0101 0010 0011 0111 0100 0110		
0000 1111 0101 0010 0011 0111 0111 0110		
0000 1111 0101 0010 0011 0111 0100 1001		



Question 3: Single Cycle Datapath & Control (13 marks)

a) Instruction ori \$s0, \$t0, 20 is executed in the above single cycle datapath. Assume the values stored in registers \$s0 and \$t0 are 7 and 9 respectively. Fill in the table with the proper <u>binary</u> numbers that correspond to the labels in the figure above. (5 marks)

А	Address of the instruction
В	
F	
G	
Ι	
Ν	

b) Complete the following table with control signal values to execute the ori instruction. 'Don't care' signals are represented by 'x'. (8 marks)

RegDst	Branch	MemRead	MemtoReg	ALU Control	MemWrite	ALUSrc	RegWrite
				Input (4 bits)			

Question 4: Multi-Cycle Datapath & Control (20 marks)

Consider implementing an imaginary R-type instruction; subtract memory (submem), in MIPS. The instruction is similar to the subtract (sub) instruction, except that it takes the second operand (i.e. the subtrahend) from the memory address stored in register rt. The instruction format and its syntax and meaning are shown below:

Field	ор	rs	rt	rd	shamt	func
Bits	31-26	25-21	20-16	15-11	10-6	5-0
submem	\$rd, \$r	s, \$rt	# \$1	d = \$rs	s – mem[[Reg[\$rt]

a) Make the necessary changes to the multicycle datapath below to support submem. (8 marks) Rules/Hints: i) No modification to the main functional units. No new control signals. You should only add wires, and/or expand existing multiplexers. ii) You may assume the ALU control module recognizes the instruction (from its func field) and supply the correct control signal to the ALU. iii) With assumption that memory access or ALU operations take one clock cycle to finish, the submem instruction takes 5 cycles to finish in the modified multicycle datatpath.



PCWrite

MemToReg

Cycle	Operations
Cycle 1	- Fetch
	- PC = PC + 4
Cycle 2	- Decode
	- Read rs and rt
	- Calculate the branch target (for possible beq)
Cycle 3	
Cycle 4	
Cycle 5	

b) Specify the operations done in each cycle in the table below. (6 marks)

c) Complete the finite state machine (FSM) diagram with the submem instruction. Remember to fill all the control signals that you have modified in part (a). (6 marks)



Question 5: MIPS Recursion (15 marks)

Fill in the blanks below to implement a <u>recursive</u> Fibonacci function in MIPS code. The C definition of the function is given below in the comments of the MIPS program. You can use any of the instructions from Appendix 1, including pseudo-instructions.

fibo:

```
#$a0 = n, $v0 = fibo(n)
#if (n==0) return 0;
#if (n==1) return 1;
#return( fibo(n-1)+fibo(n-2) );
#Step1: save preserved registers in the stack if needed
```

#Step 2: check the base case
#Jump to return0 if n==0, jump to return1 if n==1

#Step 3: handle the recursive case

#Step 4: restore the registers from stack and fib exits
exitfib:

return1:
 li \$v0,1
 j exitfib
return0:
 li \$v0,0
 j exitfib

Question 6: MIPS Programming (10 marks)

a) A single precision IEEE 754 number is stored in memory at address labelled X. Write the <u>shortest sequence</u> of MIPS instructions to multiply this number by 2, and store the result back at memory address X. Accomplish this without using any floating point instructions. You can assume no overflow happens. (4 marks)

b) Write a MIPS procedure to detect if overflow took place or not for the addition of two unsigned integers stored in registers \$t1 and \$t2.

i) Write the condition under which overflow occurs for the addition of t1 and t2 (2 marks)

ii) Provide a sequence of MIPS instructions to detect such overflow. (4 marks)

Question 7: Pipelining (15 marks)

a) The pipelined datapath that we have discussed in class is broken down into 5 steps: instruction fetch (IF), decode and register read (ID), ALU operation (EX), memory access (MEM) and result write back (WB).

Assuming each step takes a number of picoseconds $(10^{-12}s)$ to finish as follows:

IF	ID	EX	MEM	WB
305ps	275ps	280ps	305ps	250ps

i) What would be the clock cycle duration for this datapath if we want to build an efficient pipeline and why? (2 mark)

ii) In this datapath, assuming there are neither hazards nor stalls (ideal case), how long does it take to execute an instruction? (2 marks)

iii) Assuming N add instructions are executed. If they don't have any data dependencies, what is the speedup of a pipelined implementation when compared with a multi-cycle implementation with the same number of stages? Your answer should be an expression that is a function of N. (3 marks)

b) Assume we execute the following instruction sequence in the pipeline. Our pipeline uses all possible forwarding from any stage to any stage (provided it does not violate the timing consistency). Fill in the table below with the appropriate pipeline stages (IF, ID, EX, Mem, WB) or bubbles (BUB). (4 marks)

	1	2	3	4	5	6	7	8	9	10	11
sub \$s1, \$t0, \$t1	IF	ID	EX	Mem	WB						
add \$s2, \$s0, \$s1											
add \$s5, \$s3, \$s4											
add \$s6, \$s5, \$s2											

Explain every forwarding path you used to attain your answer. (4 marks)

----- End of Exam Paper ------

Appendix 1: MIPS instructions 1

				0	6	N		
M I P S	Rei	fer	ence D	ata				
CORE INSTRUCTI	ON SE	т				OPCC		
		FOR-				/ FUN		
NAME, MNEMO	NIC	MAT	OPER	ATION (in Verilog	g)	(He:		
Add	add	ĸ	R[rd] = R[rs]	+ K[rt]	(1)	0720		
Add Immediate	addi	1	R[rt] = R[rs]	+ SignExtImm	(1,2)	a _{he}		
Add Imm. Unsigned	addiu	1	R[rt] = R[rs]	+ SignExtImm	(2)	The		
Add Unsigned	addu	R	R[rd] = R[rs]	+R[rt]		0/21		
And	and	R	R[rd] = R[rs]	[& R[rt]	(2)	0724		
And Immediate	andı	1	K[rt] = K[rs]	& ZeroExtimm	(3)	che		
Branch On Equal	beq	Ι	PC=PC+4+	BranchAddr	(4)	4_{he}		
Branch On Not Equa	bne	I	if(R[rs]!=R[1 PC=PC+4+	t]) BranchAddr	(4)	$5_{\rm he}$		
Jump	j	J	PC=JumpAd	ldr	(5)	2_{he}		
Jump And Link	jal	J	R[31]=PC+8	;PC=JumpAddr	(5)	$3_{\rm he}$		
Jump Register	jr	R	PC=R[rs]			0/08		
Load Byte Unsigned	lbu	Ι	R[rt]={24'b0 +Sign),M[R[rs] 1ExtImm](7:0)}	(2)	24 _h		
Load Halfword Unsigned	lhu	Ι	R[rt]={16'b0 +Sig1),M[R[rs] hExtImm](15:0)}	(2)	25 _h		
Load Linked	11	Ι	R[rt] = M[R[rs]+SignExtImm]	(2,7)	30_{h}		
Load Upper Imm.	lui	Ι	R[rt] = {imm	ı, 16'b0}		\mathbf{f}_{he}		
Load Word	lw	Ι	R[rt] = M[R[rs]+SignExtImm]	(2)	23 _h		
Nor	nor	R	$R[rd] = \sim (R)$	[rs] R[rt])		0/27		
Or	or	R	R[rd] = R[rs]	R[rt]		0/25		
Or Immediate	ori	Ι	R[rt] = R[rs]	ZeroExtImm	(3)	d_{he}		
Set Less Than	slt	R	R[rd] = (R[rst])	$s \leq R[rt] > 1 : 0$		0/2a		
Set Less Than Imm.	slti	Ι	R[rt] = (R[rs])] < SignExtImm)?	1:0(2)	\mathbf{a}_{he}		
Set Less Than Imm. Unsigned	sltiu	Ι	R[rt] = (R[rs] < SignExtImm) ? 1 : 0	(2,6)	b_{he}		
Set Less Than Unsig.	sltu	R	R[rd] = (R[rs	s] < R[rt]) ? 1 : 0	(6)	0/21		
Shift Left Logical	sll	R	R[rd] = R[rt]	<< shamt		0/00		
Shift Right Logical	srl	R	R[rd] = R[rt]	>> shamt		0/02		
Store Byte	sb	Ι	M[R[rs]+Sig	nExtImm](7:0) =	(2)	28_{h}		
Store Conditional	SC	I	M[R[rs]+Sig	$K[rt](7:0)$ $nExtImm] = R[rt];$ $l = (atomic) ? 1 \cdot 0$	(2) (27)	38 _h		
C	11/11-224		MIR[rs]+Sig	nExtImml(15:0) =	(2,7)	00		
Store Halfword	sh	Ι		R[rt](15:0)	(2)	29 _h		
Store Word	SW	Ι	M[R[rs]+Sig	nExtImm] = R[rt]	(2)	2b _h		
Subtract	sub	R	R[rd] = R[rs]	- R[rt]	(1)	0/22		
Subtract Unsigned	subu	R	R[rd] = R[rs]	- R[rt]		0/23		
 May cause overflow exception SignExtImm = { 16{immediate[15]}, immediate } ZeroExtImm = { 16{1b'0}, immediate } BranchAddr = { 14{immediate[15]}, immediate, 2'b0 } JumpAddr = { PC+4[31:28], address, 2'b0 } Operands considered unsigned numbers (vs. 2's comp.) Atomic test&set pair; R[rt] = 1 if pair atomic, 0 if not atomic 								
BASIC INSTRUCTI	ON FC	RMA	TS					
R opcode	Г	s	rt	rd sha	nt	funct		
31 2	26 25	21	20 16	15 11 10	65			
	<u>Г</u> 26.25	S	rt	imme	ediate			
0.24 100	1. J. J.	1.2.1	20 16	12				

ARITHMETIC CO	re ins	TRU	CTION SET	OPCODE
		FOR.		/ FMT/FT / FUNCT
NAME MNEMC	NIC	MAT	OPER ATION	(Hev)
Branch On FP True	hc1t	FI	if(FPcond)PC=PC+4+BranchAddr (4)	11/8/1/
Branch On FP False	bc1f	FI	if(Pecond)PC=PC+4+BranchAddr(4)	11/8/0/
Divide	div	R	Lo=R[rs]/R[rt]; Hi=R[rs]%R[rt]	0///1a
Divide Unsigned	divu	R	Lo=R[rs]/R[rt]; Hi=R[rs]%R[rt] (6)	0///1b
FP Add Single	add.s	FR	F[fd] = F[fs] + F[ft]	11/10//0
FP Add Double	add.d	FR	${F[fd],F[fd+1]} = {F[fs],F[fs+1]} + {F[fd],F[fd+1]}$	11/11//0
FP Compare Single	CY 9*	FR	FPcond = (F[fs] on F[ft]) ? 1 : 0	$\frac{11}{10} - \frac{1}{2}$
FP Compare	04.0	IR	$FPcond = (\{FIfs\}FIfs+11\} on$	11,10, 19
Double	cx.d*	FR	{F[ft].F[ft+1]})?1:0	11/11//y
* (x is eq. 1t. 0	rle) (d	p is =	=, <, or <=) (v is 32, 3c, or 3e)	
FP Divide Single	div.s	FR	F[fd] = F[fs] / F[ft]	11/10//3
FP Divide Double	div.d	FR	{F[fd],F[fd+1]} = {F[fs],F[fs+1]} / {F[ft],F[ft+1]}	11/11//3
FP Multiply Single	mul.s	FR	F[fd] = F[fs] * F[ft]	11/10//2
FP Multiply		ED	${F[fd],F[fd+1]} = {F[fs],F[fs+1]} *$	11/11/ /2
Double	mu1.a	ГK	{F[ft],F[ft+1]}	11/11//2
FP Subtract Single	sub.s	FR	F[fd]=F[fs] - F[ft]	11/10//1
FP Subtract Double	sub.d	FR	${F[fd],F[fd+1]} = {F[fs],F[fs+1]} - {F[ft],F[fs+1]}$	11/11//1
Load FP Single	lwc1	I	F[rt]=M[R[rs]+SignExtImm] (2)	31///
Load FP	1.001	2	Firt]=MIR[rs]+SignExtImm]: (2)	
Double	ldc1	1	F[rt+1]=M[R[rs]+SignExtImm+4]	35///
Move From Hi	mfhi	R	R[rd] = Hi	0 ///10
Move From Lo	mflo	R	R[rd] = Lo	0//-12
Move From Control	mfc0	R	R[rd] = CR[rs]	10/0//0
Multiply	mult	R	${Hi,Lo} = R[rs] * R[rt]$	0///18
Multiply Unsigned	multu	R	${Hi,Lo} = R[rs] * R[rt] $ (6)	0///19
Shift Right Arith.	sra	R	R[rd] = R[rt] >>> shamt	0//-/3
Store FP Single	swc1	Ι	M[R[rs]+SignExtImm] = F[rt] (2)	39//-/
Store FP Double	sdc1	I	$ \begin{split} & M[R[rs]+SignExtImm] = F[rt]; (2) \\ & M[R[rs]+SignExtImm+4] = F[rt+1] \end{split} $	3d///

FLOATING-POINT INSTRUCTION FORMATS

FR	opc	ode	fmt	ft		fs	fd		funct
	31	26 25	21	20	16 15	11	10	65	0
FI	opc	ode	fmt	ft			immed	liate	
	31	26.25	21	20	16.15				Ô.

PSEUDOINSTRUCTION SET

NAME	MNEMONIC	OPERATION
Branch Less Than	blt	if(R[rs] <r[rt]) pc="Label</td"></r[rt])>
Branch Greater Than	bgt	if(R[rs]>R[rt]) PC = Label
Branch Less Than or Equal	ble	if(R[rs]<=R[rt]) PC = Label
Branch Greater Than or Equal	bge	if(R[rs]>=R[rt]) PC = Label
Load Immediate	li	R[rd] = immediate
Move	move	R[rd] = R[rs]

REGISTER NAME, NUMBER, USE, CALL CONVENTION

NAME	NUMBER	USE	PRESERVEDACROSS A CALL?
\$zero	0	The Constant Value 0	N.A.
\$at	1	Assembler Temporary	No
\$v0-\$v1	2-3	Values for Function Results and Expression Evaluation	No
\$a0-\$a3	4-7	Arguments	No
\$t0-\$t7	8-15	Temporaries	No
\$s0-\$s7	16-23	Saved Temporaries	Yes
\$t8-\$t9	24-25	Temporaries	No
\$k0-\$k1	26-27	Reserved for OS Kernel	No
\$gp	28	Global Pointer	Yes
\$sp	29	Stack Pointer	Yes
\$fp	30	Frame Pointer	Yes
\$ra	31	Return Address	Yes

Copyright 2009 by Elsevier, Inc., All rights reserved. From Patterson and Hennessy, Computer Organization and Design, 4th ed.

1 Ĩ Ĩ I Ĩ I

1 I Į ī

Appendix 2: MIPS instructions 2

OPCOD	ES BASE		SION	ASCIL	SVMB	IN S		3		
MIPS	(1) MIPS	(2) MIPS			Hexa-	ASCIL	Lawrence 1	Hexa-	ASCII	T
oncode	funct	funct	Binary	Deci-	deci-	Char-	Deci-	deci-	Char-	
(31.26)	(5.0)	(5.0)	Dumy	\mathbf{mal}	mal	acter	mal	mal	acter	
(1)	\$11	add.f	00 0000	0	0	NUL	64	40	(a)	+
0.5		sub.f	00 0001	1	1	SOH	65	41	Ă	
j	srl	mul.f	00 0010	2	2	STX	66	42	в	
jal	sra	div.f	00 0011	3	3	ETX	67	43	\mathbf{C}	
beq	sllv	sqrt.f	00 0100	4	4	EOT	68	44	D	1
bne		abs.f	00 0101	5	5	ENQ	69	45	E	
blez	srlv	mov.f	00 0110	6	6	ACK	70	46	F	
bgtz	srav	neg.f	00 0111	7	7	BEL	71	47	G	1
addi	jr		00 1000	8	8	BS	12	48	H	
addiu	Jair		00 1001	10	9	HI	13	49	I T	
altin	mown		00 1010	11	a b	VT	75	Ab	ĸ	
andi	syscall	round wf	00 1011	12	c	FF	76	40	T.	+
ori	break	trunc.wf	00 1101	13	ď	CR	77	4d	M	
xori		ceil.w.f	00 1110	14	e	SO	78	4e	N	
lui	sync	floor.w.f	00 1111	15	f	SI	79	4f	0	
-	mfhi		01 0000	16	10	DLE	80	50	Р	1
(2)	mthi		01 0001	17	11	DC1	81	51	Q	
	mflo	movz.f	01 0010	18	12	DC2	82	52	R	
	mtlo	movn.f	01 0011	19	13	DC3	83	53	S	
			01 0100	20	14	DC4	84	54	Т	
			01 0101	21	15	NAK	85	55	U	
			01 0110	22	16	SYN	86	56	V	
-			01 1000	23	17	EIB	8/	57	W	1
	multu		01 1000	24	10	EM	00	50	v	
	din		01 1010	25	12	SUB	00	59	7	
	divu		01 1011	27	11	ESC	91	Sh	Г Г	
	arva		01 1100	28	10	ES	92	50	1	ł
			01 1101	2.9	1d	GS	93	5d	1	
			01 1110	30	1e	RS	94	5e	7	
			01 1111	31	1f	US	95	5f		
lb	add	cvt.s.f	10 0000	32	20	Space	96	60	6	1
lh	addu	cvt.d.f	10 0001	33	21	!	97	61	а	
lwl	sub		10 0010	34	22		98	62	b	
lw	subu	<i>r</i>	10 0011	35	23	#	99	63	ç	
lbu	and	cvt.w.	10 0100	36	24	S	100	64	d	
lhu	or		10 0101	31	25	%	101	65	e	
IWr	xor		10 0110	20	20	ac ,	102	67	1	
ab	nor		10 1000	39	27		103	69	b	+
sb			10 1000	41	20	5	104	60	i	
swl	slt		10 1010	42	28	! 李	106	69	i	
SW	sltu		10 1011	43	2b	+	107	6b	k	
-			10 1100	44	2c		108	6c	1	t
			10 1101	45	2d		109	6d	m	
swr			10 1110	46	2e	8	110	6e	n	
cache			10 1111	47	2f	1	111	6f	0	
11	tge	c.f.f	11 0000	48	30	0	112	70	р	Ι
lwc1	tgeu	c.un.f	11 0001	49	31	1	113	71	q	
lwc2	tlt	c.eq.	11 0010	50	32	2	114	72	Г	
pref	tltu	c.ueq.f	11 0011	51	35	5	115	75	S	1
2 -1 - 2	teq	c.olt.	11 0100	52	34	4	110	74	τ	
1dc2	tno	c.uit.	11 0101	54	35	5	112	76	u 17	I
TUCZ	0116	C ulaf	11 0111	55	37	7	110	77	w.	I
SC		C sff	11 1000	56	38	8	120	78	x	+
swc1		c.nglef	11 1001	57	39	9	121	79	v	
swc2		c.sea.f	11 1010	58	3a	1	122	7a.	z	I
		c.ngl.f	11 1011	59	3b		123	7b	\$	I
1		c.lt.f	11 1100	60	3c	ź	124	7c	Ť	1
sdc1		c.nge.f	11 1101	61	3d	=	125	7d)	
sdc2		c.lef	11 1110	62	3e	>	126	7e	~	
		c not f	11 1111	63	3f	2	127	7f	DFI.	L

(1) opcode(31:26) == 0			
(2) opcode(31:26) == 17	ten (11hex); if fmt(25	:21)==16 _{ten} (10 _{hex})f = s (single);
if fmt(25:21)==17 _{ten}	$(11_{\text{hex}})f = d$ (double	e)	



The symbol for each prefix is just its first letter, except µ is used for micro.

Copyright 2009 by Elsevier, Inc., All rights reserved. From Patterson and Hennessy, Computer Organization and Design, 4th ed.

bottom side (columns 3 and 4) together

Fold 1

perforation to separate card