

COMP 2012H: Honors OOP and Data Structures
Fall 2015

PA3: Matrix ADT

Deadline: 11:59pm, Sunday, October 25, 2015

1 Matrix ADT

In this assignment, you are asked to implement a `Matrix` ADT. The ADT is written in a `.h` file, while the functions are fully implemented in a `.cpp` file.

The index of our matrix starts from 0, and hence an $m \times n$ matrix $A_{m \times n}$ is written as ($m, n \geq 0$)

$$A_{m \times n} = \begin{pmatrix} a_{00} & a_{01} & \cdots & a_{0,n-1} \\ a_{10} & a_{11} & \cdots & a_{1,n-1} \\ \vdots & \vdots & \ddots & \vdots \\ a_{m-1,0} & a_{m-1,1} & \cdots & a_{m-1,n-1} \end{pmatrix},$$

where $a_{i,j}$ are double numbers, and $m, n \geq 0$.

The `Matrix` class definition is as follows. You should implement your matrix as a dynamic 2-D array and provide codes for all its member functions. You **MUST** keep all the shown functions, but may add your private data members and/or member functions if you want.

```
class Matrix {                                // Matrix class
public:
    explicit Matrix(int rows = 0, int cols = 0); // constructor
    Matrix(const Matrix & mt);                // copy constructor
    ~Matrix();                                // destructor
    int rows() const;                          // return the number of rows of the matrix
    int cols() const;                          // return the number of columns of the matrix
    double & el(int i, int j) const;           // access (i, j)th element
    void assign(const Matrix & op);           // copy values from op
    Matrix mul(const Matrix & op) const;      // multiplication of matrices
    Matrix transpose() const;                 // the transpose of matrix
    Matrix inverse() const;                   // the inverse of matrix

    // Add your public member functions, if any, in the following
private:
    double **elm;                             // matrix elements
    int r;                                     // number of rows
    int c;                                     // number of columns
    // Add your private data members and private member functions,
    // if any, in the following
};
```

The member functions are explained as follows.

1. Constructor:

```
// Constructor: Initialize the matrix to be a rows x cols matrix.
// rows >= 0; cols >= 0
// default is an empty 0 x 0 matrix
// No need to initialize matrix elements
Matrix::Matrix(int rows, int cols) {
```

2. Copy constructor:

```
// Copy constructor
Matrix::Matrix(const Matrix & mt) {
```

3. Destructor.

```
// Destructor for the matrix
Matrix::~Matrix() {
```

4. Inspector function for row:

```
// Return the number of rows of the matrix
int Matrix::rows() const {
```

5. Inspector function for column:

```
// Return the number of columns of the matrix
int Matrix::cols() const {
```

6. Element access:

```
// Return the (i, j)th element of the matrix
// Precondition: i and j are valid ranges
double & Matrix::el(int i, int j) const {
```

7. Assignment function, to copy all elements in matrix op. That is, a call of A.assign(B) will copy element by element from matrix B to A.

Note that you need to resize the matrix before copying so that the new matrix is of the same dimension as op.

```
// Assign and copy all the elements of matrix op to the matrix.
// Resize matrix (allocate space) if necessary
void Matrix::assign(const Matrix & op) {
```

8. Matrix multiplication, where a call of `A.mul(B)` returns a new matrix which is the product of matrices `A` and `B`.

Matrix multiplication is defined as follows. The product of two matrices $A_{m \times p}$ (with entries a_{ij}) and $B_{p \times n}$ (with entries b_{ij}) is a $C_{m \times n}$ matrix whose entries c_{ij} is given by

$$c_{ij} = \sum_{k=0}^{p-1} a_{ik}b_{kj}, \quad \forall 0 \leq i < m, 0 \leq j < n.$$

```
// Return a new matrix which is the product of
// this matrix and matrix op.
// Precondition: valid multiplication with correct rows and columns
Matrix Matrix::mul(const Matrix & op) const {
```

9. Transpose operation, which returns a new matrix which is the transpose of this matrix.

Matrix $B_{n \times m}$ is the transpose of matrix $A_{m \times n}$ iff

$$b_{ji} = a_{ij}, \quad \forall 0 \leq i < m, 0 \leq j < n.$$

```
// Return a new matrix which is the transpose of the matrix.
Matrix Matrix::transpose() const {
```

10. Inverse: Matrix B is the inverse of a square matrix A iff $AB = I$. If A does not have an inverse, please return a zero matrix. (For a discussion on how to invert a matrix, you may consult http://www.mathwords.com/i/inverse_of_a_matrix.htm)
Hint: The Adjoint method described in the webpage is easier to implement than the others.

```
// Return a new matrix which is the inverse of the matrix.
// Return a zero matrix if inverse does not exist
Matrix Matrix::inverse() const {
```

2 What to be turned in

Provide us your header file `Matrix.h` and the implementation file `Matrix.cpp`. We will include your `Matrix.h` and write our own tester to test-run your program. However, if you have a tester file, please provide to us as well.

3 Extra Credits (Maximum 10%)

There are many other matrix operations, such as eigenvectors, eigen-values, solution of $Ax = b$, etc. Implement what you know about matrix operations to gain extra credits here (at the discretion of the grader). Please explain the extras you have done in your README.